

Hierarchical sequence-affinity landscapes shape the evolution of breadth in an anti-influenza receptor binding site antibody

Angela M. Phillips^{1,2*†}, Daniel P. Maurer^{3,4*}, Caelan Brooks⁵, Thomas Dupic¹, Aaron G. Schmidt^{3,4}, Michael M. Desai^{1,5,6,7†}

¹Department of Organismic and Evolutionary Biology, Harvard University, Cambridge MA 02138,

²Department of Microbiology and Immunology, University of California, San Francisco, CA 94143, ³Ragon

institute of MGH, MIT, and Harvard, Cambridge MA 02139, ⁴Department of Microbiology, Harvard

Medical School, Boston, MA 02115, ⁵Department of Physics, Harvard University, Cambridge, MA 02138,

⁶NSF-Simons Center for Mathematical and Statistical Analysis of Biology, Harvard University, Cambridge

MA 02138, ⁷Quantitative Biology Initiative, Harvard University, Cambridge MA 02138.

*These authors contributed equally to this work.

†angela.phillips@ucsf.edu, mdesai@oeb.harvard.edu

Abstract

Broadly neutralizing antibodies (bnAbs) that neutralize diverse variants of a particular virus are of considerable therapeutic interest¹. Recent advances have enabled us to isolate and engineer these antibodies as therapeutics, but eliciting them through vaccination remains challenging, in part due to our limited understanding of how antibodies evolve breadth². Here, we analyze the landscape by which an anti-influenza receptor binding site (RBS) bnAb, CH65, evolved broad affinity to diverse H1 influenza strains^{3,4}. We do this by generating an antibody library of all possible evolutionary intermediates between the unmutated common ancestor (UCA) and the affinity-matured CH65 antibody and measure the affinity of each intermediate to three distinct H1 antigens. We find that affinity to each antigen requires a specific set of mutations – distributed across the variable light and heavy chains – that interact non-additively (*i.e.*, epistatically). These sets of mutations form a hierarchical pattern across the antigens, with increasingly divergent antigens requiring additional epistatic mutations beyond those required to bind less divergent antigens. We investigate the underlying biochemical and structural basis for these hierarchical sets of epistatic mutations and find that epistasis between heavy chain mutations and a mutation in the light chain at the V_H-V_L interface is essential for binding a divergent H1. Collectively, this work is the first to comprehensively characterize epistasis between heavy and light chain mutations and shows that such interactions are both strong and widespread. Together with our previous study analyzing a different class of anti-influenza antibodies⁵, our results implicate epistasis as a general feature of antibody sequence-affinity landscapes that can potentiate and constrain the evolution of breadth.

Introduction

The diversity of influenza poses an ongoing public health challenge, as vaccination and natural infection typically elicit immune responses that are highly strain-specific, and hence quickly lose efficacy as the virus evolves⁶⁻⁹. This limited efficacy has garnered substantial interest in vaccination strategies that elicit broadly neutralizing antibodies (bnAbs) that neutralize diverse strains of influenza^{1,7}. Over the past two decades, there has been considerable effort to isolate and characterize anti-influenza bnAbs^{3,10-12}. These bnAbs target various conserved epitopes on the hemagglutinin (HA) influenza surface glycoprotein, including the receptor binding site (RBS)³, the stem or stalk domain¹¹⁻¹³, the lateral patch¹⁴, and the

48 membrane-proximal anchor site¹⁵. BnAbs also vary in germline gene usage and breadth, with some
49 binding several strains within an HA subtype and others binding nearly all characterized influenza
50 strains¹.

51

52 Despite the immense body of work on influenza bnAbs, we still do not fully understand the evolutionary
53 processes through which they mature^{16,17}. Our strategies to elicit them therefore remain limited. It is clear,
54 however, that distinct, but clonally related sequences can target the same HA epitope and confer
55 functionally similar breadth⁴. This redundancy suggests that there are many possible evolutionary
56 pathways to influenza bnAbs. Still, the relatively low frequencies at which they are observed in human
57 repertoires following vaccination suggest that there are factors constraining their maturation that we do
58 not yet fully appreciate¹⁸⁻²².

59

60 High-throughput mutagenesis approaches are widely used as a tool to understand key properties shaping
61 the evolution of numerous proteins²³⁻²⁶. This work has revealed that new mutations can differentially
62 impact distinct protein functions, and often interact non-additively (*i.e.*, *epistatically*), potentially
63 constraining the order in which they can occur²⁷⁻²⁹. For antibodies, high-throughput mutagenesis studies
64 have largely been limited to examining the effects of single mutations, either through saturating
65 mutagenesis (*e.g.*, deep mutational scanning) of relatively small regions^{18,30,31} or through random
66 mutagenesis (*e.g.*, error-prone PCR)³²⁻³⁴. These methods examine the local mutational landscape of a
67 particular antibody, or in other words, how single mutations can change affinity or breadth. The advantage
68 of these methods is that the sequences analyzed are relatively unbiased, particularly for saturating
69 mutagenesis, and thus one can surmise why particular mutations occurred naturally. For example, this
70 approach identified many single amino acid substitutions in the anti-influenza bnAb C05 that improve
71 affinity to different subsets of strains but typically reduce breadth¹⁸.

72

73 A key limitation of saturating mutagenesis approaches is that they cannot probe how epistatic interactions
74 between mutations might constrain antibody evolutionary trajectories, which typically involve multiple
75 mutations³⁵. Because antibodies acquire numerous mutations and experience fluctuating selection
76 pressures on short timescales^{35,36} they are necessarily distinct from other proteins for which epistasis has
77 been studied. Moreover, they bind antigens through disordered loops, in contrast to the structured active
78 sites of most enzymes, and they are relatively tolerant to mutations³⁷⁻⁴¹. Further, the evolutionary
79 dynamics of affinity maturation are defined by discrete rounds of mutation and selection, compared to
80 the more continuous processes most proteins are subject to, and thus mutations that occur concurrently
81 are selected based on their collective rather than individual effects^{35,42}. For these reasons, the
82 evolutionary constraints on antibodies may be unique.

83

84 The few studies that have examined epistasis in antibodies indicate that it is a key determinant of
85 affinity^{4,5,43,44}. For example, multiple studies have identified mutations that interact synergistically to bind
86 an antigen^{4,5,43}. Still, most of this work has focused on interactions between a small subset of mutations⁴.
87 Addressing the prevalence and general importance of epistasis in shaping antibody evolution will require
88 more comprehensive combinatorial mutagenesis strategies that sample combinations of mutations
89 present in each somatic antibody sequence⁵. These combinatorial strategies, however, do not capture
90 epistasis with other mutations that could have occurred in alternative evolutionary pathways, which will
91 require integrating combinatorial mutagenesis with the saturating mutagenesis methods described
92 above.

93

94 In previous work, we systematically mapped the relationship between antibody sequence and affinity (the
95 sequence-affinity landscape) across mutational landscapes relevant for the somatic evolution of two
96 stem-targeting bnAbs of varying breadth, CR6261 and CR9114⁵. We found that affinity was determined
97 by non-additive interactions between mutations, and that such epistasis could both constrain and
98 potentiate the acquisition of breadth. Notably, the nature of this epistasis varied considerably between
99 the two bnAbs. For CR6261, epistatic interactions were similar for binding distinct group 1 strains, thus
100 evolutionary pathways could simultaneously improve in affinity to divergent antigens. For CR9114,
101 increasingly divergent antigens required additional epistatically interacting mutations such that
102 evolutionary pathways were constrained to improve in affinity to one antigen at a time. The distinct
103 topologies of these sequence-affinity landscapes result from differences between the various antigens
104 and the mutations that are required for binding.

105
106 Although anti-stem bnAbs are among the broadest influenza bnAbs characterized, they are a small and
107 biased subset of the influenza antibody response. Despite the presence of anti-stem antibodies in human
108 sera⁴⁵ and the ability to drive viral escape mutants *in vitro*⁴⁶, the stem is minimally mutated amongst
109 circulating viral strains and does not appear to be evolving in response to these antibodies, possibly due
110 to the high concentration of antibody required for protection^{47,48} and likely immune pressure. In contrast,
111 due to the small size of the RBS pocket, RBS-directed bnAbs frequently make contacts with
112 immunodominant epitopes surrounding the pocket that have substantial antigenic variation^{3,49-52}.
113 Although RBS-directed bnAbs have a relatively narrower reactivity profile compared to anti-stem bnAbs,
114 they are potently neutralizing, do not require effector functions for potent *in vivo* protection as do anti-
115 stem bnAbs^{11,53}, and have evolved broad recognition despite the accumulation of antibody escape
116 mutations in the periphery of the RBS. Further, RBS-directed bnAbs can mature from diverse germline
117 V_H and V_L genes⁴⁹, suggesting there are likely numerous evolutionary pathways to target this epitope.
118 Thus, to understand more generally how epistasis constrains bnAb evolution, here we consider RBS-
119 directed bnAbs, as they target an entirely different epitope under distinct immune selection pressures.

120
121 Specifically, we examine the influence of epistasis on the evolution of a well-characterized RBS-directed
122 bnAb, CH65, which binds and neutralizes diverse H1 strains^{3,4}. CH65 was isolated from a donor seven
123 days post-vaccination. The unmutated common ancestor (UCA) and an early intermediate (I-2) have
124 moderate affinity for a subset of H1 strains that circulated early in the donor's lifetime^{3,4}. The affinity-
125 matured CH65 has 18 mutations throughout the light (V_L) and heavy (V_H) variable regions, which improve
126 affinity to strains that circulated early in the donor's life and confer affinity to antigenically drifted strains^{4,54}.
127 Thus, CH65 evolved to acquire affinity to emerging strains without compromising affinity for previously
128 circulating strains.

129
130 The structural changes upon affinity maturation of CH65 and clonally related antibodies have been
131 extensively characterized^{3,4,55}. This work showed that CH65 primarily matures by preconfiguring the
132 HCDR3 loop into its binding conformation, thereby minimizing the conformational entropic cost of
133 binding⁴. Importantly, none of the 18 somatic mutations are in the HCDR3; rather, key mutations in
134 HCDR1, HCDR2, and LCDR1 result in contacts that stabilize the HCDR3 loop in its binding compatible-
135 conformation^{4,54}. This structural characterization, in addition to molecular dynamics simulations, identified
136 specific mutations that are critical for breadth, including some that interact synergistically to stabilize the
137 HCDR3 loop^{4,54}. In theory, such epistasis could constrain bnAb evolution by requiring multiple mutations
138 to confer a selective advantage, or alternatively, it could compensate for the deleterious effects of other
139 mutations and favor selection of bnAbs.

140

141 Given that many mutations in CH65 are important for imparting affinity to HA, including those at distant
142 sites⁴, we hypothesized that there are many sets of epistatic mutations in CH65 not previously identified,
143 particularly because long-range epistatic interactions are difficult to predict from structural analyses
144 alone. In contrast to the anti-stem bnAbs described above^{12,56}, CH65 engages HA through both light and
145 heavy chain contacts and requires mutations in both chains to bind divergent antigens^{4,54}. Thus, it is likely
146 that mutations interact epistatically both within and between the heavy and light chains. Despite the
147 potential importance of these interactions in shaping the evolution of CH65, and the numerous other
148 antibodies that engage antigens using both chains^{11,55,57,58}, characterizations of inter-chain epistasis have
149 so far been limited to small sets of a few mutations^{4,54}. Although these smaller datasets have revealed
150 some important inter-chain epistatic interactions, they measure a subset of interactions selected based
151 on structural data, and thus we still do not know the magnitude or prevalence of this epistasis and hence
152 how important it is in shaping antibody evolution.

153
154 Here, to elucidate the role of epistasis (both inter- and intra-chain) in shaping the evolution of an RBS
155 antibody, we systematically characterize the CH65 sequence-affinity landscape. Specifically, we
156 generate a combinatorially complete antibody library containing all possible evolutionary intermediates
157 between the unmutated common ancestor (UCA) and the mature somatic sequence ($N = 2^{16} = 65,536$)
158 and measure affinity to three antigenically distinct H1 strains to assess how epistasis can shape
159 evolutionary pathways leading to varying levels of breadth. We find that strong high-order epistasis
160 constrains maturation pathways to bind antigenically distinct antigens. Although fewer epistatic mutations
161 are needed to bind an antigen similar to that bound by the UCA, these sets of mutations overlap with
162 those required to bind a more divergent antigen. Collectively, these landscapes provide mechanistic
163 insight into how affinity maturation responds to an evolving epitope and how exposure history can
164 influence future immune responses. In combination with our previous work on anti-stem bnAbs⁵, this work
165 shows how epistasis can differentially impact the evolutionary trajectories of bnAbs of varying breadth,
166 epitope, and variable chain gene-usage.

167

168

169 Results

170

171 To comprehensively examine how epistasis may have shaped the evolution of CH65, we generated a
172 combinatorially complete antibody library comprising all possible evolutionary intermediates from the
173 UCA to CH65. This library contains all possible combinations of mutations present in both the variable
174 heavy and light chains of CH65, less two mutations (Q1E and S75A) distant from the paratope that do
175 not significantly impact binding affinity (**Figure 1A, Figure 1–figure supplement 1**) or physically interact
176 with other residues. Removing these mutations results in a final library size of 2^{16} , which is within the
177 throughput limit of our methods.

178

179 To profile the breadth of the corresponding antibody library, we first transform this combinatorial plasmid
180 library into yeast for antibody surface display in a single-chain variable fragment (scFv) format⁵⁹. We then
181 use Tite-Seq³⁰, a high-throughput method that couples flow cytometry with sequencing, to measure
182 equilibrium binding affinities to three H1 strains bound by CH65. We chose these strains to sample
183 varying levels of antigenic change^{36,60}: they include a strain that circulated early in the donor's lifetime
184 (A/Massachusetts/1/1990, "MA90") and a strain that circulated 16 years later (A/Solomon Islands/3/2006,
185 "SI06")⁴. Additionally, because affinity maturation has been shown to confer binding to antigens that
186 escape less mutated members of the same lineage⁶¹, we drove viral escape of MA90 *in vitro* using the
187 UCA and found that CH65 could bind to the resulting strain (A/Massachusetts/1/1990 G189E, "MA90-

188 G189E”) that escapes the UCA (**Figure 1A**). We use the MA90-G189E antigen to profile incremental
 189 antigenic change from MA90 (one direct escape mutation), whereas SI06 represents more substantial
 190 antigenic change during natural evolution, including loss of K133a and the mutation E156G in the RBS.
 191
 192 For each of these three antigens, we used Tite-Seq to measure equilibrium binding affinities for all 2^{16}
 193 variants in biological duplicates (**Figure 1 – figure supplement 2**). We log-transform the binding affinities
 194 and report $-\log K_D$, which is proportional to the free energy change of binding (and is thus expected to
 195 combine additively)^{62,63}. For each antigen, the Tite-Seq $-\log K_D$ correlate well between replicates ($r \sim 0.99$
 196 for all antigens) and accurately reflect isogenic measurements made by flow cytometry ($r = 0.98$; **Figure**
 197 **1–figure supplement 3B**) as well as recombinant IgG affinity measurements made by biolayer
 198 interferometry ($r = 0.89$; **Figure 1–figure supplement 3C**).
 199

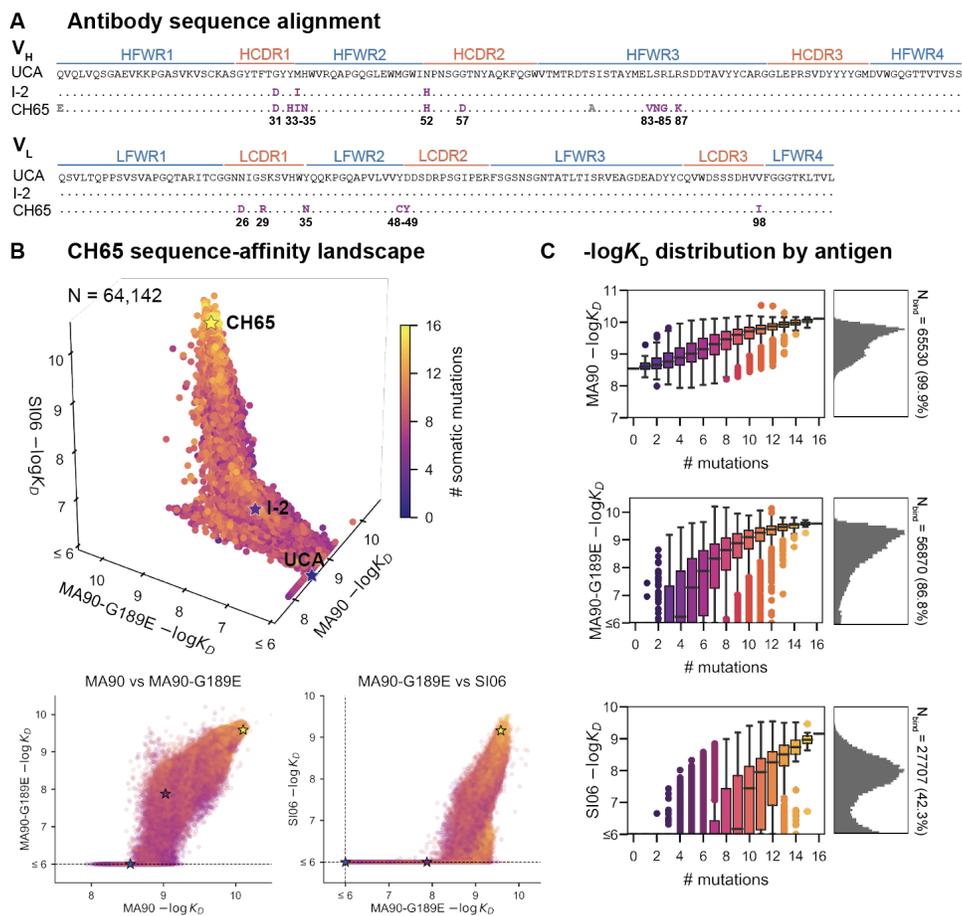


Figure 1. CH65 sequence-affinity landscape. (A) Alignment of UCA, I-2, and CH65 V_H (top) and V_L (bottom) sequences. Mutations of interest are shown in purple and are numbered; gray mutations do not impact affinity and were excluded from the library. **(B)** $-\log K_D$ for $\sim 2^{16}$ variants to each of the three antigens. Each point is colored by the number of somatic mutations in the corresponding variant. The UCA, I-2, and CH65 are annotated as stars; N = 64,142 after filtering poor K_D measurements from the Tite-Seq data (see Methods). Two-dimensional representations of the data are shown below the three-dimensional plot. **(C)** Distribution of $-\log K_D$ for each antigen. Left: variant $-\log K_D$ grouped by the number of somatic mutations; Right: $-\log K_D$ histograms for variants that bind each antigen, with total number of binding variants (N) indicated on plot. **Figure 1 – figure supplement 1.** CH65 mutation reversion. **Figure 1 – figure supplement 2.** Tite-Seq workflow and sorting scheme. **Figure 1 – figure supplement 3.** Tite-Seq K_D quality control and isogenic measurements. **Figure 1 – figure supplement 4.** CH65 library expression. **Figure 1–source data 1.** Tite-Seq K_D and expression measurements. **Figure 1–source data 2.** Isogenic K_D and expression measurements.

200 Broadly, we find that increasingly divergent antigens require additional mutations to confer antigen
 201 binding. Consistent with previous work^{4,54}, the UCA has weak affinity for MA90 but does not bind MA90-
 202 G189E or SI06; I-2 has improved affinity to MA90, weak affinity to MA90-G189E, and does not bind SI06;
 203 and CH65 has near maximal affinity amongst library variants for all three antigens (**Figure 1B**). While the
 204 entire library binds MA90, ~87% of variants bind MA90-G189E, and ~42% of variants bind SI06 (**Figure**
 205 **1C**). For all antigens, affinity is higher for more mutated variants, except for a subset of highly-mutated
 206 variants that do not bind SI06 (**Figure 1B**, bottom right). There are ~2,000 variants that bind MA90 with
 207 reduced affinity relative to the UCA; none of these variants have detectable affinity for SI06, and only
 208 ~0.4% have detectable affinity for MA90-G189E (**Figure 1B**). Further, all variants that bind SI06 also bind
 209 MA90-G189E (**Figure 1B**), as variants can bind MA90-G189E with fewer mutations than SI06 (**Figure**
 210 **1C**). This “hierarchical” or “nested” pattern, where mutations that enable binding to more antigenically
 211 divergent strains are dependent on mutations that enable binding to less divergent strains, is reminiscent
 212 of what we observed previously for the anti-stem bnAb CR9114⁵, despite the comparatively subtle
 213 differences between the antigens examined here (83 - 96% epitope identity versus 52 - 61% for the
 214 CR9114 antigens)^{12,55}.
 215
 216 To understand how specific mutations shape the sequence-affinity landscape, we computed the change
 217 in affinity resulting from each of the 16 mutations on all 2¹⁵ (32,768) genetic backgrounds at the other 15
 218 sites. This analysis reveals that several mutations improve affinity to MA90 and MA90-G189E (e.g.,
 219 Y35N, Y48C, D49Y, G31D, Y33H, H35N, N52H), and some of these distributions are multimodal,
 220 indicating that their effect on affinity depends on the presence of other mutations (**Figure 2A**). Consistent
 221 with this, some mutations improve affinity on the UCA or I-2 backgrounds (e.g., Y35N, Y33H, H35N) and
 222 others on the CH65 background (Y48C, D49Y). For SI06, N52H dramatically improves affinity and most
 223 variants lacking this mutation do not have detectable affinity. Thus, several mutations (e.g., Y35N)
 224 improve affinity to SI06 in the I-2, but not the UCA, background (**Figure 2A**). In general, the effects of

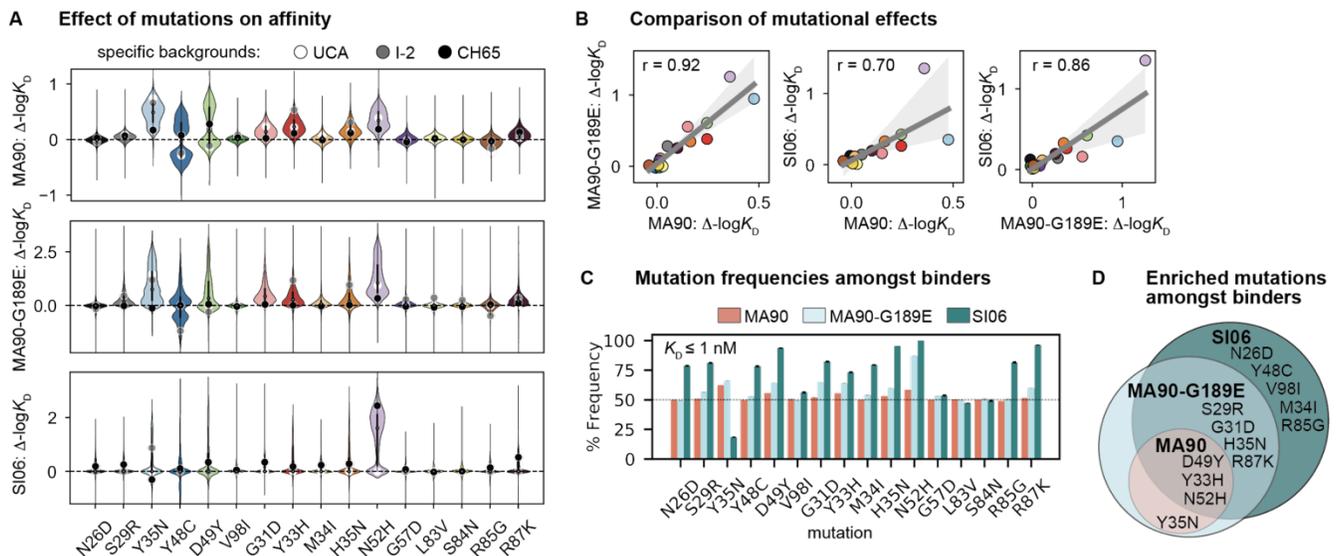


Figure 2. Mutational effects on affinity. (A) Change in $-\log K_D$ resulting from each mutation on all 32,768 genetic backgrounds. Impact of mutation on the UCA, I-2, and the CH65 genetic backgrounds are represented by white, gray, and black points, respectively. (B) Correlation of mean effect on $-\log K_D$ for MA90, SI06, and MA90-G189E resulting from each mutation. Regression line and 95% confidence intervals are shown in gray. Mutations are colored as in (A). (C) Frequency of each mutation amongst variants that bind a given antigen with $K_D \leq 1$ nM. Error bars correspond to standard deviation across bootstrapped data ($N = 10$). (D) Mutations present at $> 55\%$ frequency (p -value < 0.05 from one-sided t -test) amongst binders for each antigen. **Figure 2 – figure supplement 1.** Change in $-\log K_D$ resulting from each mutation as a function of the number of other mutations present.

225 these mutations correlate between the different antigens, with mutations affecting affinity more
226 substantially for MA90-G189E and SI06 compared to MA90 (**Figure 2B**).

227

228 To assess which mutations confer affinity to a particular antigen, we computed the frequency of each
229 mutation amongst binding variants in the library. Consistent with the landscapes in **Figure 1B**, we
230 observe that the mutations enriched amongst binders form a hierarchical pattern between the antigens
231 (**Figure 2C**). For example, a few mutations are enriched ($\geq 55\%$ frequency) amongst variants with
232 nanomolar affinity for MA90 (e.g., Y35N, D49Y, Y33H, N52H), a few additional mutations are enriched
233 amongst MA90-G189E binders (e.g., S29R, G31D, H35N, R87K), and still additional mutations are
234 enriched amongst SI06 binders (e.g., N26D, Y48C, V98I, M34I, R85G) (**Figure 2D**). Thus, except for
235 Y35N, which is interestingly depleted amongst SI06 binders (**Figure 2 – figure supplement 1**), the
236 mutations that enhance affinity to the three antigens form a hierarchical pattern.

237

238 We next characterized how epistasis between these mutations might impact affinity and result in this
239 hierarchical pattern of breadth. To this end, we fit our measured $-\log K_D$ to a standard biochemical model
240 of epistasis²⁹, which is a linear model defined as the sum of single mutational effects and epistatic terms
241 up to a specified order (see Methods). Using a cross-validation approach, we find that the optimal order
242 model for affinity to each of these antigens is fifth-order, and we report coefficients at each order from
243 these best-fitting fifth-order models (**Figure 3A**). The magnitude and sign of these coefficients correspond
244 to effects on $-\log K_D$: for example, a second-order term of +1 means that two mutations occurring together
245 improve $-\log K_D$ by 1 unit, beyond the sum of their first-order effects. For all three antigens, we find
246 widespread epistasis between mutations in the same chain and between mutations in different chains,
247 with many epistatic terms exceeding first-order effects in magnitude (**Figure 3**). In contrast to our previous
248 work on variable heavy-chain only antibody landscapes⁵, we find many strong epistatic interactions
249 between mutations that are too distant to physically interact (**Figure 3 – figure supplements 1-4**).

250

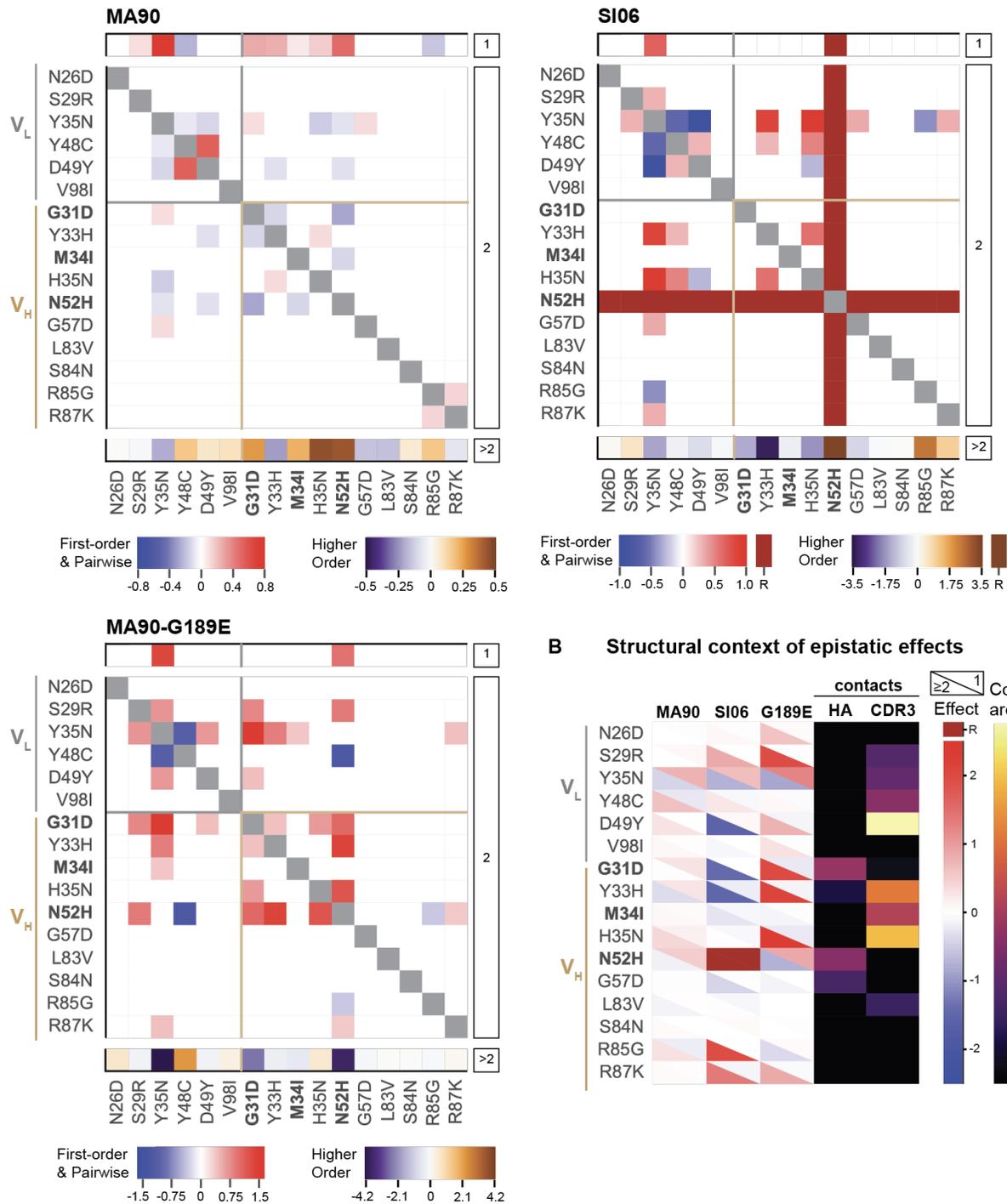
251 Because there are substantial long-range epistatic interactions, our combinatorial approach identifies
252 numerous interactions not previously known, in addition to confirming the few interactions characterized
253 in earlier work (e.g., Y48C and D49Y have strong synergistic epistasis)^{4,54}. Here we find strong epistasis
254 between the I-2 mutations (G31D, M34I, N52H), neighboring mutations (Y33H, H35N), mutations known
255 to stabilize light chain contacts (Y48C, D49Y)⁴, as well as an uncharacterized light chain mutation (Y35N).
256 When we examine the structural context of this epistasis, we find that mutations with strong linear and
257 epistatic effects often make contact with either HA or with the HCDR3 that engages the RBS (**Figure**
258 **3B**). This suggests that the effects of these mutations are either mediated through the contacts that they
259 make with HA, or through affecting the HCDR3 loop conformation. These mutations interact epistatically
260 for each of the three antigens, though the magnitude of epistasis is higher for SI06 (explaining ~36%
261 of the variance in K_D , relative to ~24% for MA90 and ~26% for MA90-G189E, see **Figure 3 – figure**
262 **supplement 5**).

263

264 Importantly, these epistatic interactions are essential for the acquisition of affinity to both MA90-G189E
265 and SI06. To investigate the molecular details of this epistasis, we compared the crystal structures of the
266 unbound UCA, I-2, and CH65 as well as CH65 bound to SI06^{3,4,64}. Additionally, we produced several
267 variants as recombinant IgG to assay the binding kinetics by biolayer interferometry. To mimic the Tite-
268 seq system, IgG was bound to biosensors and assayed for binding to full-length trimeric HA (**Figure 4 –**
269 **figure supplement 2-4**). Here, we focus on binding kinetics of minimally mutated variants that confer
270 affinity to each antigen but binding of twelve variants was assayed to all three antigens at varying
271 temperatures (**Figure 4—figure supplement 5**).

272

A First-order, pairwise, and higher-order mutational effects



B Structural context of epistatic effects

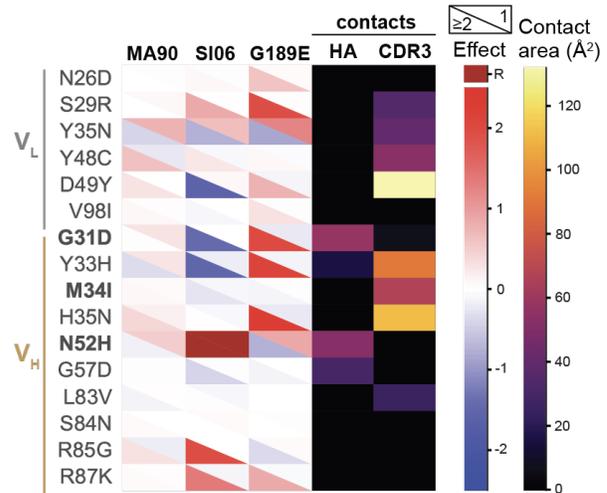


Figure 3. Epistatic coefficients for biochemical model of epistasis. (A) First-order, pairwise, and higher-order mutational effects for each of the 16 mutations inferred from the optimal order model for each antigen. Higher-order effects are reported as a sum. Mutations present in I-2 are shown in bold. ‘R’ indicates that the mutation is required for binding (defined as being present in $\geq 90\%$ of binding variants) and is thus excluded from the epistasis inference. **(B)** Structural context of linear and epistatic effects. For each mutation, the upper triangle shows the first-order effect, the lower triangle shows the sum of the pairwise and higher-order effects, and the contact surface area with HA and HCDR3 are shown in the fourth and fifth columns. **Figure 3 – figure supplement 1.** Pairwise effects versus distance. **Figure 3 – figure supplement 2.** Biochemical epistasis within heavy and light chains and between chains. **Figure 3 – figure supplement 3.** Epistatic coefficients for statistical epistasis model. **Figure 3 – figure supplement 4.** Comparison of coefficients in biochemical and statistical models. **Figure 3 – figure supplement 5.** Variance partitioning for statistical epistasis model. **Figure 3 – source data 1.** Coefficients for biochemical epistatic model.

273 The I-2 intermediate (which contains G31D, M34I, N52H) is amongst the least-mutated variants that binds
 274 MA90-G189E (**Figure 1B**). The N52H mutation, which substantially improves affinity to MA90-G189E
 275 (**Figure 4A**), would potentially clash with one of the binding-incompatible HCDR3 conformations
 276 observed in crystal structures of the UCA and I-2, thus this mutation potentially increases the occupancy
 277 of the binding-compatible HCDR3 conformation (**Figure 4—figure supplement 1A**). In the bound state,
 278 N52H forms π -stacks with Y33H and hydrogen bonds with G31D (**Figure 4B, 4C, Figure 4—figure**
 279 **supplement 1B**). Consequently, N52H and G31D, which together interact to provide high affinity for
 280 MA90-G189E (**Figure 4A**), form a network of interactions between HCDR1, HCDR2, and the 150-loop
 281 of HA to stabilize the binding interaction (**Figure 4B, 4C**). Thus, while N52H alone confers affinity to
 282 MA90-G189E, G31D and M34I (I-2) reduce the dissociation rate by ~ 3.5 -5 fold to improve affinity (**Figure**
 283 **4C, Figure 4—figure supplement 5**). Notably, these interactions are distant from the site of viral escape

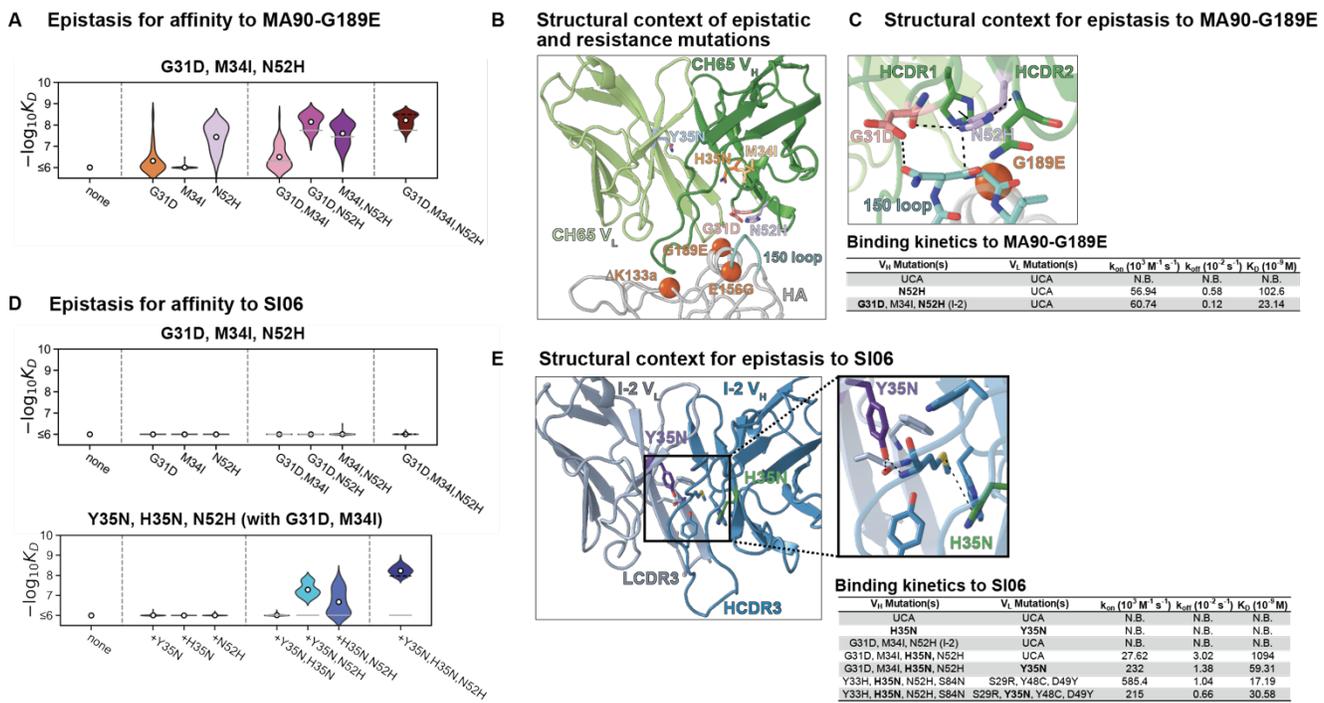


Figure 4. Structural basis of epistasis in CH65. (A) Epistasis between three mutations in I-2 (G31D, M34I, N52H) determines affinity to MA90-G189E. (B) Epistatic mutations that confer affinity to viral escape strains are distant from the sites of escape. Shown is CH65 bound to SI06 (PDB 5UGY³). Colored residues highlight the locations of the mutations shown in A and C. Spheres highlight the locations of the viral escape mutations (G189E, Δ K133a, and E156G). (C) Top: Mutations N52H and G31D establish a network of interactions between HCDR1, HCDR2, and HA. Bottom: Binding kinetics against MA90-G189E for select variants at 30 °C by biolayer interferometry using a bivalent analyte binding model. (D) Mutations in I-2 are insufficient for affinity to SI06 (top) but interact epistatically with Y35N and H35N to bind SI06 (bottom). (E) Left: Epistatic mutations Y35N and H35N are located at the VH-VL interface. Right: Somatic mutations remove interactions with the HCDR3. Shown is the unbound I-2 structure (PDB 4HK3⁴). Bottom: Binding kinetics against SI06 for select variants at 30 °C by biolayer interferometry using a bivalent analyte binding model. **Figure 4 – figure supplement 1.** In CH65, the N52H mutation moves relative to the UCA and I-2 and clashes with unbound HCDR3 conformations observed in the UCA and I-2. **Figure 4 – figure supplement 2.** Representative biolayer interferometry (BLI) traces and bivalent analyte fits against MA90. **Figure 4 – figure supplement 3.** Representative BLI traces and bivalent analyte fits against MA90-G189E. **Figure 4 – figure supplement 4.** Representative BLI traces and bivalent analyte fits against SI06. **Figure 4 – figure supplement 5.** Summary of all association rates, dissociation rates, and dissociation constants measured by BLI against MA90, MA90-G189E, and SI06 at multiple temperatures. **Figure 4 – figure supplement 6.** BLI traces and fits of the antibody variant containing the I-2 mutations with H35N and Y35N. **Figure 4 – figure supplement 7.** X-ray data collection and refinement statistics for unbound Fabs. **Figure 4 – source data 1.** Binding kinetics for selected antibody variants determined by biolayer interferometry.

284 (G189E, **Figure 4B, 4C**). Though these mutations are also important for affinity to the antigenically drifted
285 SI06, they are insufficient to confer binding in the absence of other epistatic mutations (**Figure 4D**, top).
286

287 In examining the minimally mutated variants that can bind SI06, we find that Y35N in the light chain and
288 H35N in the heavy chain interact synergistically with the I-2 mutations (G31D, M34I, N52H) to confer
289 affinity to SI06 (**Figure 4D**, bottom). Thus, the hierarchical sets of mutations that confer broad reactivity
290 to these antigens (**Figure 2D**) do so through epistasis. In particular, the germline residue Y35 in the light
291 chain framework (FWR) 2 is part of a cluster of aromatic residues at the V_H - V_L interface and makes π -
292 stacking, methionine-aromatic, and hydrogen bonding interactions between LFWR2 and LCDR3,
293 HCDR3, and HFWR4 (**Figure 4E**). The somatic mutation Y35N effectively removes these interactions
294 with the HCDR3. Although the loss of the aromatic moiety from tyrosine to asparagine likely has a
295 destabilizing effect, we attribute the observed changes in affinity to the loss of hydrogen bonding between
296 LFWR2 and HCDR3; this is in part because the lineage member CH67, which has similarly broad
297 reactivity, acquires a Y35F mutation upon affinity maturation which is only a removal of a hydroxyl group⁴.
298 Similarly, H35N removes a methionine-aromatic interaction, known to have a stabilizing effect in
299 proteins⁶⁵, between the HFWR2 and HCDR3 (**Figure 4E**). Addition of Y35N and H35N into the UCA
300 background did not confer affinity to SI06 (**Figure 4D, 4E**). However, the addition of H35N into the I-2
301 background produced weak but detectable affinity with an association rate that was improved upon
302 addition of Y35N (**Figure 4E, Figure 4—figure supplement 6**). Notably, while Y35N confers affinity to
303 SI06 for variants with few somatic mutations, the magnitude of this effect diminishes as the number of
304 mutations increases. Indeed, Y35N is depleted amongst the highest affinity variants (**Figure 2C, Figure**
305 **2—figure supplement 1**) and in the context of a mutated background decreased the association rate
306 and overall affinity (**Figure 4E**), suggesting that Y35N, which removes inter-chain contacts, is likely only
307 beneficial during early rounds of affinity maturation.
308

309 Because previous studies on this lineage^{4,54} identified HCDR3 rigidification as a mechanism for binding
310 to SI06, we determined x-ray crystal structures of unbound Fabs containing Y35N in the UCA background
311 or Y35N and H35N in the I-2 background and compared them to previously determined structures (**Figure**
312 **4—figure supplement 1C**). These variants were insufficient to rigidify the HCDR3 as observed by the
313 HCDR3 conformation and high B factors or the lack of density corresponding to the HCDR3 (**Figure 4—**
314 **figure supplement 1C**). These data show that I-2 mutations conferred affinity towards MA90-G189E by
315 stabilizing the HCDR1 and HCDR2 with HA and were required for the addition of Y35N and H35N, which
316 remove contacts with HCDR3, to confer affinity against SI06 without complete HCDR3 rigidification,
317 revealing a biophysical mechanism through which inter-chain epistasis can determine broad affinity in a
318 hierarchical manner.
319

320 The extent of epistasis we observe suggests that the evolution of CH65 is contingent on mutations
321 occurring in a particular order. Further, the hierarchical pattern of mutations that confer affinity to the
322 different antigens indicates that the likelihood a mutation fixes depends on the selecting antigen. Because
323 we measured affinities for a combinatorially complete library, we can infer the likelihood of all possible
324 evolutionary trajectories from the UCA to CH65 (with and without the constraint of passing through the I-
325 2 intermediate) in the context of various possible antigen selection scenarios (*e.g.*, maturation to MA90
326 alone, or to SI06 alone, etc.). To this end, we implement a framework in which the probability of any
327 mutational step is higher if $-\log K_D$ increases and lower if $-\log K_D$ decreases (see Materials and methods)⁵.
328 We use $-\log K_D$ to each antigen to compute the likelihood of all possible mutational trajectories in the
329 context of each of the antigens, as well as in the context of all possible sequential selection scenarios,
330 where the selecting antigen can change. We focus on scenarios involving the two antigens that the donor

331 was likely exposed to (**Figure 5**) – MA90 early in their life and SI06 later in their life – but we also perform
 332 this analysis with the MA90-G189E data (**Figure 5 – Figure supplement 1**). Additionally, we consider
 333 selection resulting from a mixture of antigens, which we approximate by randomly selecting an antigen
 334 for each mutational step⁶⁶ and average this pathway likelihood over 1000 random draws.
 335

336 This pathway likelihood inference reveals that mutational trajectories leading to CH65 are most favorable
 337 in sequential selection scenarios that begin with MA90 and end with SI06, consistent with the donor's
 338 likely exposure history^{4,55}. This order is preferred irrespective of passing through the I-2 intermediate, and
 339 in fact the exact same selection scenario (four mutations selected with MA90 followed by 12 mutations
 340 selected with SI06) is the most likely scenario regardless of whether paths are constrained to pass
 341 through I-2 (**Figure 5A**). Further, the MA90-SI06 sequential scenarios are considerably more likely than
 342 either antigen alone, a mixture of antigens, or SI06-MA90 sequential scenarios.
 343

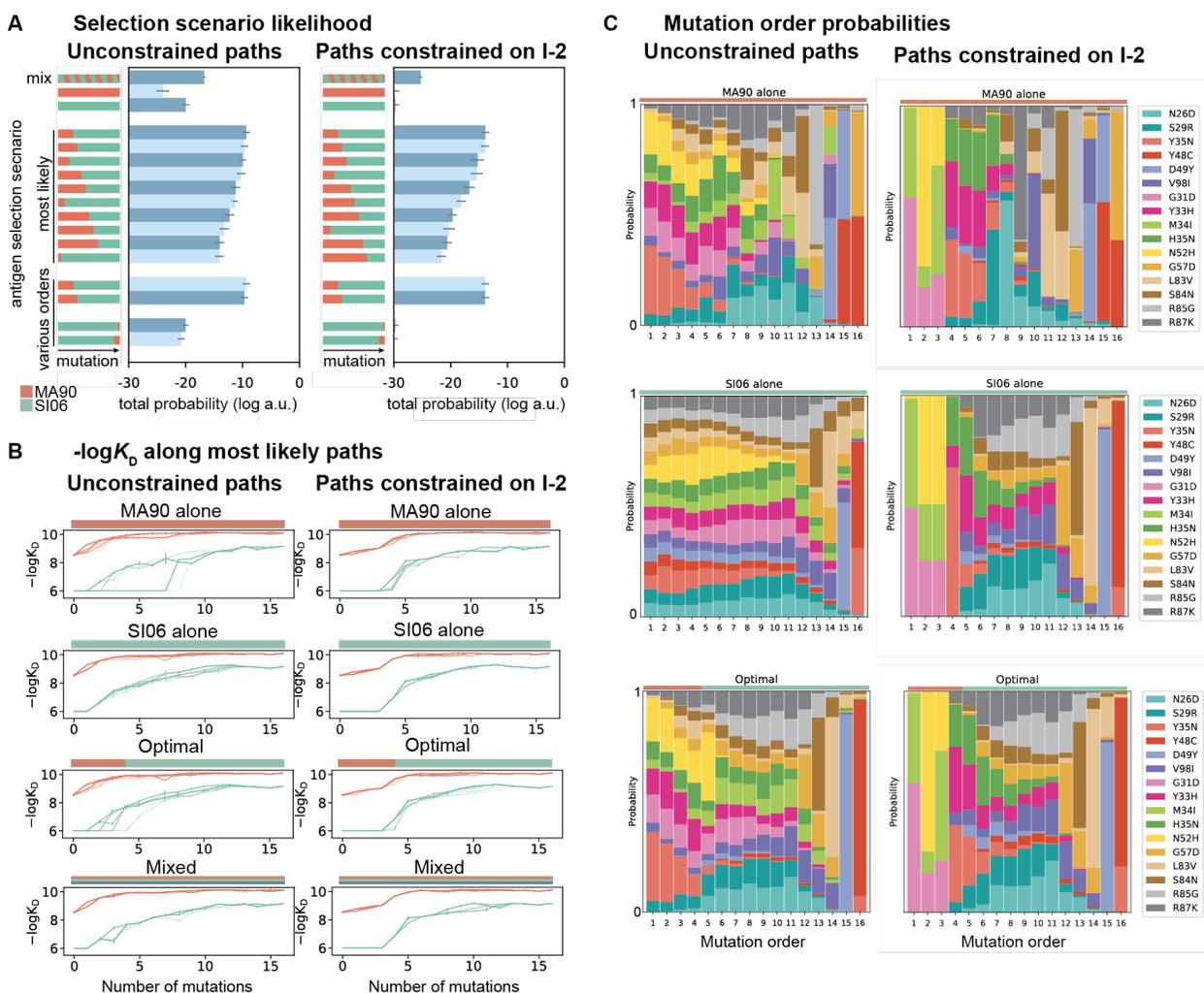


Figure 5. Antigen selection scenarios and likely mutational pathways. (A) Selection scenario likelihood. Total probability of all mutational paths (left) or all paths that pass through I-2 (right) assuming specific antigen selection scenarios are shown. **(B)** $-\log K_D$ for 25 most likely paths under designated antigen selection scenarios are shown with (right) and without (left) the constraint of passing through I-2. **(C)** Probability of each mutation occurring at a specific order under select antigen selection scenarios, with (right) and without (left) the constraint of passing through I-2. **Figure 5 – figure supplement 1.** Antigen selection scenarios and likely mutational pathways with MA90, SI06, and MA90-G189E. **Figure 5 – figure supplement 2.** Likelihood of passing through specific 3-mutation intermediates.

344 These drastic differences in scenario likelihood result from the effects of specific mutations on various
345 genetic backgrounds. Mutations on the UCA background can improve affinity to MA90 but not to SI06,
346 so MA90 is favored as the selecting antigen initially. After a few mutations, however, MA90 reaches
347 maximal affinity and cannot improve further, at which point mutations begin to improve SI06 affinity. Thus,
348 SI06 is favored later in mutational trajectories (**Figure 5B**). These constraints reflect the structure of the
349 sequence-affinity landscape: selection with MA90 favors mutations that enable the acquisition of SI06
350 affinity and would be unlikely to occur under selection with SI06 alone. Similarly, when we consider all
351 three antigens, we find that scenarios that begin with MA90 or MA90-G189E and end with SI06 are most
352 likely, again reflecting the hierarchical nature of the sequence-affinity landscape (**Figure 5–figure**
353 **supplement 1**).

354
355 We also leverage our combinatorial data to infer the probability of each mutation occurring at a given
356 step along the evolutionary pathway from UCA to CH65 (**Figure 5C**). Even when we do not constrain
357 pathways to pass through I-2, we find that the I-2 mutations and epistatic mutations that interact with the
358 HCDR3 (*e.g.*, Y33H, H35N and the previously uncharacterized Y35N) are most likely to occur early in
359 mutational trajectories, especially in scenarios that begin with MA90 selection. Additionally, the highly
360 synergistic HCDR3-stabilizing mutations Y48C and D49Y are most likely to occur late, and consecutively,
361 with D49Y preceding the otherwise-deleterious Y48C. These general trends are robust to constraining
362 paths to pass through the I-2 intermediate. Consistent with our structural analyses, we find that when
363 pathways are constrained to pass through I-2, Y35N is the most probable subsequent mutation, and this
364 likelihood rapidly decreases with additional mutations. However, when we consider all possible pathways
365 in the optimal antigen selection scenario, I-2 is not the most likely 3-mutation intermediate, suggesting
366 that the evolution of CH65 was not contingent on passing through I-2 (**Figure 5–figure supplement 2**).
367 Still, the likelihood of passing through the I-2 intermediate is twice that expected by chance– it is a
368 minimally mutated antibody with improved affinity to MA90 and MA90-G189E, and it contains the N52H
369 mutation that is essential for SI06 affinity. Thus, while there are many accessible paths to CH65, the three
370 mutations in I-2 result in rapid improvements in affinity and breadth and favor subsequent selection for
371 epistatic mutations that ultimately provide the breadth of CH65.

372
373

374 Discussion

375

376 Collectively, we find that the breadth of an RBS influenza bnAb, CH65, is determined by high-order
377 epistatic interactions that differ between divergent antigens. This epistasis is widespread within and
378 between both the heavy and light chains. To our knowledge, this is the first comprehensive study of inter-
379 chain epistasis and illustrates the extent to which mutations can differentially impact affinity depending
380 on the presence of other mutations, even those too far apart to physically interact. This suggests that the
381 maturation of antibodies that engage antigen with both chains may be distinct compared to those that do
382 not. There are more opportunities for epistatic interactions across two chains compared to just one, and
383 the degree of both intra- and inter-chain epistasis is likely contingent on the chain pairing. Given the
384 importance of both light and heavy chain mutations across diverse bnAbs^{11,55,57,58}, understanding the
385 nature of this epistasis may be useful for designing therapeutic antibodies and eliciting broadly protective
386 immune responses.

387

388 Further, our structural analysis shows that the epistasis that confers broad reactivity in this antibody is
389 mediated through sets of mutations that both interact with HA and those that do not interact with HA.
390 These epistatic mutations add or remove interactions between CDRs, FWRs, and chains that act by

391 different mechanisms of stabilizing the binding conformation (e.g., G31D and N52H) or removing
392 constraints on the HCDR3 (e.g., Y35N and H35N). The Y35N mutation effectively removes interactions
393 between the LFWR2 and the HCDR3 at the V_H - V_L interface and mediates affinity improvement to a more
394 antigenically advanced influenza strain by increasing the association rate. An analogous observation was
395 noted for the anti-HIV bnAb CH103 that co-evolved during a natural infection within in a single individual⁶⁷.
396 Structural studies of CH103 identified mutations at the V_H - V_L interface (which is the region containing
397 residue 35 in CH65) that were associated with reconfiguration of the HCDR3 to enable broad reactivity
398 against a viral escape variant⁶⁸. Although additional work will be needed to address the generality of this
399 finding, it appears that antibodies can evolve to bind viral escape variants by modulating the V_H - V_L
400 interface and the HCDR3 configuration, in response to both chronic (HIV) and punctuated (influenza)
401 exposures. While Y35N is advantageous early in affinity maturation, it becomes detrimental in highly
402 mutated backgrounds that have undergone HCDR3 rigidification. Consequently, Y35N may function to
403 initially increase flexibility, enabling acquisition of affinity to SI06 after acquiring mutations in the heavy
404 chain, and subsequent maturation rigidified the HCDR3. This increased flexibility followed by rigidification
405 is reminiscent of molecular dynamics studies of anti-HIV bnAbs that suggest initial increases in flexibility
406 may provide a means to sample additional conformational space prior to rigidification⁶⁹.

407
408 In comparing CH65 mutations that improve affinity to diverse H1 antigens, we find that increasingly
409 divergent antigens require additional epistatically interacting mutations, resulting in a hierarchical pattern
410 of mutations that improve affinity to distinct antigens. The I-2 mutations (e.g., G31D, M34I, N52H) may
411 compensate for the G189E mutation by stabilizing interactions with HA opposite this site, potentially
412 allowing the antibody to shift to relieve the clash; a similar observation was made for another RBS-
413 directed antibody⁷⁰. These same mutations help to stabilize binding in the antigenically distant SI06 but
414 do not sufficiently compensate for the loss of potential contacts between the HCDR3 and the RBS (e.g.,
415 Δ K133a and E156G) within the antigen combining site; further mutations Y35N and H35N that likely
416 influence HCDR3 conformations are needed. These structural observations and the data generated here
417 suggest that mutations confer broad reactivity in the CH65 lineage in a hierarchical manner. Although the
418 hierarchical landscape of CH65 is not as striking as that of CR9114⁵, where larger sets of mutations are
419 required to bind substantially more divergent antigens, it is intriguing that the landscape for a considerably
420 narrower bnAb can also have this structure. This suggests that hierarchical sequence-affinity landscapes
421 may be quite common, as they are not unique to CR9114, to anti-stem bnAbs, or to bnAbs that engage
422 distinct HA subtypes.

423
424 If hierarchical sequence-affinity landscapes are common amongst bnAbs, they may contribute to the low
425 frequencies of bnAbs in human repertoires. For bnAbs with such landscapes, epistatically interacting
426 mutations are required to bind a given antigen, additional epistatic mutations (that interact favorably with
427 those acquired previously) are required to bind a distinct antigen, and so on. Determining how this might
428 constrain bnAb evolution will require assessing how rare these sets of synergistic mutations are.
429 Importantly, the landscapes measured here and in our previous work focus exclusively on mutations
430 present in the affinity-matured antibodies, which are biased by the selection pressures those bnAbs
431 experienced. Thus, while these landscapes show that diverse bnAbs can mature by acquiring hierarchical
432 sets of epistatic mutations that are favored in sequential exposure regimens, there may be alternative
433 mutational pathways to breadth that are not hierarchical and are favored in other exposure regimes.

434
435 Still, the observation that antibodies *can* evolve breadth through hierarchical mutational landscapes lends
436 support for vaccination with sequential doses of distinct antigens. These findings are consistent with a
437 recent study that demonstrates memory B cell recruitment to secondary germinal centers upon

438 vaccination in humans, allowing for additional rounds of antibody maturation to antigenically drifted
439 strains⁷¹. Here we find that sequential exposures with antigenically drifted strains may help elicit within-
440 subtype potent bnAbs like CH65, in addition to the cross-subtype bnAbs described in our previous work.
441 Several theoretical and computational models of bnAb affinity maturation also favor sequential
442 immunization strategies, as they allow antibodies to acquire the mutations necessary to bind one antigen
443 before experiencing selection pressure to bind another, ultimately producing bnAbs that have 'focused'
444 on conserved epitopes^{66,72-75}. Our work indicates that this focusing process may occur by favoring
445 selection on hierarchical sets of epistatically interacting mutations. We note that while the hierarchical
446 epistasis we observe favors the acquisition of breadth to a set of specific antigens, antagonistic epistasis
447 between these mutations and new mutations could prevent the acquisition of breadth to other antigens.
448 Further, both CH65 and CR9114 have higher affinity to the strain most like the inferred original
449 immunogenic stimulus, and weaker affinity to more divergent strains^{12,55}. This is consistent with the
450 concept of immunological imprinting or original antigenic sin, where antibodies boosted upon vaccination
451 or infection typically have high affinity for the eliciting strain⁷⁶. Although we show that the CH65 antibody
452 lineage can evolve breadth that compensates for viral escape mutations, the affinities are lower for more
453 antigenically distant strains, suggesting that there is likely a trade-off between antibody breadth and
454 affinity. Further work will be needed to assess whether RBS-targeting bnAbs like CH65, which target
455 highly variable epitopes compared to stem-targeting bnAbs^{4,55}, can mature to bind substantially divergent
456 strains (e.g., post-pandemic H1N1 strains that CH65 does not effectively neutralize), or whether historical
457 contingency prevents them from doing so.

458
459 Finally, although epistasis can make evolution more difficult to predict^{77,78}, the general patterns of
460 epistasis emerging from these combinatorial landscapes suggest that there are indeed broadly applicable
461 insights. For example, these hierarchical synergistic interactions reveal how epistasis constrains the
462 evolution of antibody affinity, breadth, and trade-offs between the two. Moving forward, additional
463 combinatorial antibody libraries will advance our understanding of how pervasive these features are – for
464 example, for antibodies that target distinct viruses. Ultimately, though, to understand why we observe
465 these particular bnAbs and not others, we need to explore the unobserved regions of sequence space.
466 We also need to assess the numerous other properties that likely impact selection on antibodies (e.g.,
467 stability, folding, polyreactivity). Thus, integrating approaches such as this combinatorial approach with
468 methods for assessing local mutational landscapes (e.g., deep mutational scanning) and methods to
469 measure other antibody properties in high-throughput will provide a more comprehensive view of the
470 factors that constrain and potentiate antibody evolution.

471

472 **Materials and Methods**

473

474 **Antibody library production**

475

476 **Antibody sequences and mutations of interest**

477 The UCA860 amino acid sequence³ was codon-optimized for expression in yeast. Amino acid
478 substitutions corresponding to those in CH65 were encoded by ≥ 2 nucleotide mutations, when possible.
479 The V98I mutation, which lies outside the region captured by 2x250 bp reads, was encoded by a
480 synonymous mutation at Arg53. The Q1E and S75A mutations in V_H were determined to minimally
481 influence affinity (**Figure 1–figure supplement 1**) and were excluded from all subsequent experiments
482 to reduce the library size.

483

484 **Yeast display plasmid and strains**

485 Single-chain variable format (scFv) antibody constructs were cloned via Gibson Assembly⁷⁹ into the
486 pCHA yeast display vector⁸⁰ with a C-terminal myc epitope tag and Aga-2 fusion (Supplementary Files
487 1-2). These scFv constructs were displayed on the surface of the EBY100 yeast strain⁵⁹, as described
488 below for the yeast library production. Unless otherwise noted, yeast were cultured by rotating at 30°C
489 and were pelleted by centrifuging at 14,000 x g (1 min) or 3,000 x g (10 min).

490

491 **Combinatorial Golden Gate Assembly**

492 To assemble the combinatorially complete library containing all $2^{16} = 65,536$ variants, the scFv sequence
493 was sectioned into five fragments of roughly equal length such that each fragment contained ≤ 5
494 mutations. Primers were designed to create all possible ($\leq 2^5$) versions of each fragment by adding
495 mutations, a Bsa-I cleavage site, and a 4-bp overhang unique to each fragment (Supplementary File 3).
496 Fragments were amplified from the UCA860 sequence via PCR using Q5 Polymerase (NEB, Ipswich,
497 MA, #M0491). The resulting fragments were purified using a 2X ratio of Aline beads (Aline Biosciences,
498 Woburn, MA, #C-1003-5), overnight DpnI digestion at 37°C (NEB #R0176), and a second 2X ratio bead
499 cleanup. The backbone vector was prepared by replacing the scFv sequence in the pCHA yeast display
500 vector with a *ccdB* counter-selection marker. Equimolar amounts of each fragment were then pooled, and
501 assembled into the backbone vector at a 2:1 molar ratio via Golden Gate Assembly⁸¹ (NEB #R3733). The
502 assembly mix was then transformed into electrocompetent DH10B *E. coli* in 5 x 25 μ L cell aliquots (NEB
503 #C3020). Each cell aliquot was recovered in 1 mL outgrowth media at 37°C for 1 hr and then transferred
504 into 100 mL of molten LB (1% tryptone, 0.5% yeast extract, 1% NaCl, 100 g/L ampicillin (VWR # V0339),
505 0.4% SeaPrep agarose (VWR, Radnor, PA #12001-922) in a 500 mL baffled flask. The bacteria-agar
506 mixture was incubated at 4°C for three hours to gel the agar and was then incubated at 37°C for 16 hours.
507 Each flask contained 1-2 million colonies (5-10 million colonies across five flasks; > 100 times the library
508 diversity) and was blended by shaking at 200 rpm for 1 hour. The cells were then pelleted by spinning at
509 3,000 x g for 10 minutes, and plasmid DNA was extracted using the ZymoPURE II Plasmid Midiprep Kit
510 (Zymo Research, Irvine, CA, #D4201).

511

512 **Yeast library production**

513 One day prior to transformation, EBY100 cells were thawed by inoculating 5 mL YPD (1% Bacto yeast
514 extract (VWR #90000-726), 2% Bacto peptone (VWR #90000-368), 2% dextrose (VWR #90000-904))
515 with 150 μ L glycerol stock and rocking at 30°C for 12-24 hr. The scFv plasmid library was then
516 transformed into EBY100 cells by the lithium acetate method⁸² and transformants were recovered in 100
517 mL molten SDCAA (1.71 g/L YNB without amino acids and ammonium sulfate (Sigma-Aldrich, St. Louis,
518 MO, #Y1251), 5 g/L ammonium sulfate (Sigma-Aldrich #A4418), 2% dextrose (VWR #90000-904), 5 g/L

519 Bacto casamino acids (VWR #223050), 100 g/L ampicillin (VWR # V0339), 0.4% SeaPrep agarose (VWR
520 #12001–922)) in 500 mL baffled flasks. The yeast-agar mixture was incubated at 4°C for 3 hours to allow
521 the agar to set and was then incubated at 30°C for 48 hours to allow for yeast colony growth. Each flask
522 contained ~700,000 colonies, totaling about 7 million colonies across ten flasks (> 100 times the library
523 diversity). After disrupting the agar by shaking at 200 rpm for 1 hr, the yeast library was inoculated into
524 liquid SDCAA (1.71 g/L YNB without amino acids and ammonium sulfate (Sigma-Aldrich #Y1251), 5 g/L
525 ammonium sulfate (Sigma-Aldrich, MO, #A4418), 2% dextrose (VWR #90000–904), 5 g/L Bacto
526 casamino acids (VWR #223050), 100 g/L ampicillin (VWR # V0339), 5.4 g Na₂HPO₄ (Sigma-Aldrich,
527 #S7907), 8.56 g NaH₂PO₄·H₂O (Sigma-Aldrich, #S9638))⁸³ and grown for five generations to saturation
528 before freezing at -80°C in 1 mL aliquots containing 5% glycerol.

529

530 **Viral Escape**

531

532 **Cell lines and media**

533 HEK293T cells were passaged in DMEM (Gibco, #11965126) supplemented with 10% fetal bovine serum
534 (Peak Serum) and Penicillin-Streptomycin (Gibco, #15140163) subsequently referred to as “D10”.
535 MDCK-SIAT1 cells (Sigma, #05071502) were passaged in D10 additionally supplemented with 1 mg/ml
536 Geneticin (Gibco, #10131035). Prior to infection, Geneticin was not included in the MDCK-SIAT1
537 medium. Media used to propagate influenza, referred to as “flu media”, contains Opti-MEM (Gibco,
538 #31985088) supplemented with 0.3% BSA (Roche, #03117332001), 0.01% FBS, and Penicillin-
539 Streptomycin. Prior to propagation, 1 µg/ml of TPCK-trypsin (Sigma, #T1426) was freshly added to flu
540 media.

541

542 **Generation of recombinant MA90 virus**

543 We used a standard eight plasmid reverse genetics system⁸⁴ to generate a recombinant 6:2 virus bearing
544 the PB2, PB1, PA, NP, M, and NS genomic segments from PR8 (A/Puerto Rico/8/1934; a kind gift from
545 Jesse Bloom), MA90 HA (Genbank: L19027), and A/Siena/10/1989 NA (Genbank: CY036825). Because
546 the sequencing of the MA90 HA was not complete, the C-terminus was extended with that of
547 A/Siena/10/1989 (Genbank: CY036823). In a six-well plate treated with poly-L-lysine (Sigma, #P4707),
548 6 x 10⁵ HEK293T cells and 1 x 10⁵ MDCK-SIAT1 cells were added to wells six-well plates in D10. The
549 next day, media was aspirated from the cells and fresh, pre-warmed D10 was added on top. For each
550 transfection, 8 µL of Trans-IT LT1 (Mirus, #2300) was added to Opti-MEM (Gibco, #31985070) containing
551 0.5 µg of each plasmid and incubated at room temperature for 20 minutes. The mixture was then added
552 dropwise to the cells. After ~5 hours, the media was aspirated from the cells and flu media freshly
553 supplemented with 1 µg/ml TPCK-treated trypsin was added. After two days, dead cells were removed
554 from the virus-containing media by centrifugation at 800 x g for 5 minutes. The supernatant was then
555 supplemented with 1 µg/ml TPCK-treated trypsin and added to a confluent monolayer of MDCK-SIAT1
556 cells seeded one day before in a six well plate and washed once with PBS (seeded at 7 x 10⁵ cells per
557 well). After ~4-5 hours, the supernatant was removed, and fresh flu media supplemented with 1 µg/ml
558 TPCK-treated trypsin was added. One day later, successful rescue was judged by observing cytopathic
559 effect. Multiple rescue transfections were pooled and added to 10 cm dishes containing a confluent
560 monolayer of MDCK-SIAT1 cells seeded one day prior (at 3 x 10⁶ cells per dish) as detailed above. Two
561 days later, successful propagation was judged by cytopathic effect, the supernatant was clarified by
562 centrifugation, and aliquots were frozen at -80 °C.

563

564

565

566 **Escape variant generation**

567 Prior to infection, MA90 virus was incubated with a low concentration of antibody (started at 0.01 µg/ml
568 of the UCA), a higher concentration of antibody (one half-log greater than the lower concentration), or no
569 antibody (as a control for cell line adaptation mutations) in 500 µL of flu media supplemented with 1 µg/ml
570 TPCK-treated trypsin for 1 hour at 37 °C and 5% CO₂. MDCK-SIAT1 cells seeded the day before were
571 washed with PBS and then virus-antibody mixtures were added to the monolayers and incubated for 1
572 hour at 37 °C and 5% CO₂, rocking the plate every ~15 minutes to ensure that the cells did not dry out.
573 Afterwards, the viral inoculum was removed, and the cells were washed with PBS before adding fresh flu
574 media supplemented with 1 µg/ml TPCK-treated trypsin. After 2 days, viral growth was judged by
575 cytopathic effect. The well that grew with a higher concentration of antibody was selected for the next
576 passage where the “low” antibody concentration was the same as the previous passage and the “high”
577 concentration was a half-log higher. This process was repeated until viral growth was readily detectable
578 at 100 µg/ml of the UCA. If necessary, a hemagglutination assay using turkey red blood cells (Lampire,
579 #7249409) was run to determine whether virus was present. Briefly, two-fold dilutions of the virus in PBS
580 were mixed with 0.5% turkey red blood cells and incubated at room temperature for at least 30-45 minutes
581 before visualization of red blood cell pellets to determine whether virus had grown significantly. Once the
582 virus still grew in 100 µg/ml of the antibody, the virus was passaged one additional time and 100 µg/ml
583 of antibody was additionally added to the media added after infection. The RNA from the escaped virus
584 was isolated using a QIAamp viral RNA mini kit (Qiagen, #52904), and the full-length HA was amplified
585 using gene-specific primers and the OneStep RT-PCR kit (Qiagen, #210212). The resulting PCR product
586 was sequenced by Sanger sequencing (Genewiz). The mutation G189E was identified from the
587 sequencing results and produced as a recombinant protein for subsequent experiments (see below).

588

589 **Antigen and IgG production**

590

591 **Choice of HA antigens**

592 Antibodies CH65, CH66, and CH67 were isolated from plasmablasts from donor TIV01⁸⁵ after receiving
593 the trivalent influenza vaccine in the 2007-2008 influenza season which contained the A/Solomon
594 Islands/3/2006 (SI06) H1N1 strain. The donor TIV01 was born in ~1990 and subsequent work identified
595 that the inferred UCA of this lineage bound to the strain A/Massachusetts/1/1990 (MA90) circulating near
596 the donor’s birth date and is suspected to be highly similar to the original immunogenic stimulus of this
597 lineage⁵⁵. However, the UCA did not bind SI06 which escaped the UCA and I-2 of this lineage⁵⁵. To
598 assess whether affinity maturation in this lineage is capable of accommodating for an escape mutation
599 that abrogates binding to less mature variants, we drove viral escape from MA90 *in vitro* (see above)
600 using the UCA and identified that matured variants of this lineage (e.g., CH65 and CH67) bound the
601 escape variant (MA90-G189E) with high affinity. To understand how this antibody lineage evolved to
602 compensate for viral escape mutations, we included MA90-G189E and SI06 in addition to MA90.

603

604 **Recombinant protein cloning, expression, and purification**

605 Variable heavy and light chains were synthesized as eBlocks (IDT). Full-length, codon-optimized HAs
606 (A/Massachusetts/1/1990 - MA90, MA90-G189E, and A/Solomon Islands/03/2006 - SI06) and full-length
607 human IgG1 heavy and light chains were cloned into a pVRC expression vector containing a C-terminal
608 HRV 3C cleavage site, His tag, FoldOn trimerization domain, and AviTag for HAs and a HRV 3C cleavage
609 site followed by a C-terminal His tag for antibody heavy chains. Recombinant proteins were produced in
610 Expi293F cells (Gibco, #A14527) following the manufacturer’s directions. The trimeric HAs were purified
611 from the supernatant using TALON metal affinity resin (Takara, #635653), washing with PBS, and eluting
612 with PBS containing 200 mM imidazole (pH 7.4). After concentration, proteins were further purified over

613 an S200 column on an AKTA pure (Cytiva). For yeast surface display assays, the HAs were further
614 biotinylated and flash-frozen in liquid nitrogen (see below). For kinetics measurements, the HAs were
615 used within two weeks of production and never frozen.

616
617

618 **HA biotinylation**

619 Biotinylation of the HAs was performed using the BirA500 kit (Avidity) following the manufacturer's
620 instructions. To compensate for the reduced activity in PBS, twice the amount of BirA was added and the
621 reaction was additionally supplied with twice the amount of biotin using the supplied BIO-200. The
622 biotinylation reaction was allowed to proceed for 1.5 hours at 30°C before 0.2 µm filtering and purification
623 over an S200 column (Cytiva). The trimeric HAs were then concentrated and flash-frozen in liquid
624 nitrogen for single-use aliquots. Biotinylated HAs were quality controlled by a gel shift assay.
625 Approximately 2 µg of biotinylated HA was heated in non-reducing Laemmli buffer (Bio-Rad, #1610737)
626 at 95°C for 5 minutes. Once cooled to room temperature, excess streptavidin was added and allowed to
627 incubate for at least 5 minutes. As a control, samples were run with PBS added rather than streptavidin.
628 The mixture was then run on a Mini-PROTEAN TGX Stain-Free gel (Bio-Rad, #4568096) and imaged.
629 All biotinylated HAs shifted in the presence of streptavidin, indicating successful biotinylation.

630

631 **Tite-Seq assays**

632

633 Tite-Seq assays were performed in biological duplicate (on different days) for each antigen, as previously
634 described^{5,30} with some modifications described below.

635

636 **Induction of antibody expression**

637 On day 1, the yeast CH65 library and isogenic strains containing the pCHA-UCA860 or pCHA-CH65
638 plasmids were thawed by inoculating 5 mL SDCAA with 150 µL glycerol stock and rotating at 30°C for 24
639 hr. On day 2, yeast cultures were back-diluted to OD600 = 0.2 in 5 mL SDCAA and rotated at 30°C until
640 they reached an OD600 = 0.4 - 0.6 (about four hours). Subsequently, 1.5 mL of these log-phase cultures
641 were pelleted, resuspended in 4 mL SGDCAA (1.71 g/L YNB without amino acids and ammonium sulfate
642 (Sigma-Aldrich #Y1251), 5 g/L ammonium sulfate (Sigma-Aldrich, MO, #A4418), 1.8% galactose (Sigma-
643 Aldrich #G0625), 0.2% dextrose (VWR #90000-904), 5 g/L Bacto casamino acids (VWR #223050), 100
644 g/L ampicillin (VWR # V0339), 5.4 g Na₂HPO₄ (Sigma-Aldrich, #S7907), 8.56 g NaH₂PO₄·H₂O (Sigma-
645 Aldrich, #S9638))⁸³, and rotated at room temperature for 20-22 hr.

646

647 **Primary antigen labeling**

648 On day 3, following induction of scFv expression, cultures were pelleted, washed twice with cold 0.1%
649 PBSA (VWR #45001-130, GoldBio, St. Louis, MO, #A-420-50), and resuspended to an OD600 of 1. For
650 each concentration of antigen (0.75-log increments spanning 1 µM - 1 pM), 700 µL of the CH65 yeast
651 library (OD600 = 1) were incubated with biotinylated HA by rocking at 4°C for 24 hr. Notably, the volume
652 of each antigen concentration was adjusted such that the number of antigen molecules exceeded that of
653 antibody molecules by at least ten-fold (assuming 50,000 scFv/cell)⁵⁹.

654

655 **Secondary fluorophore labeling**

656 On day 4, yeast-HA complexes were pelleted at 4°C and washed twice with 5% PBSA + 2 mM EDTA.
657 Complexes were then incubated with Streptavidin-RPE (1:100, Thermo Fisher Scientific, Waltham, MA,
658 #S866) and anti-cMyc-FITC (1:50, Miltenyi Biotec, Somerville, MA, #130-116-485) at 4°C for 45 min in

659 the dark. Following incubation, complexes were washed twice with 5% PBSA + 2 mM EDTA and stored
660 on ice in the dark until sorting.

661

662 **Sorting**

663 Yeast-HA complexes were sorted on a BD FACS Aria IIIu equipped with an 85 micron fixed nozzle and
664 405 nm, 440 nm, 488 nm, 561 nm, and 635 nm lasers. Single-color controls were used to compensate
665 for minimal overlap between the FITC and PE channels. For all sorts, single cells were gated by FSC vs
666 SSC, and the resulting population was sorted either by expression (FITC) or HA binding (PE). For the
667 expression sort, ~1.6 million (~20X library diversity) single cells were sorted into four gates of equal width
668 spanning the FITC-A axis. For the HA binding sort, ~1.6 million scFv-expressing cells were sorted into
669 four gates spanning the PE-A axis, with one gate capturing all PE-negative cells, and the remaining three
670 each capturing 33% of the PE-positive cells (**Figure 1–figure supplement 2**). All cells were sorted into
671 5 mL polypropylene tubes containing 1 mL of 2X SDCAA supplemented with 1% BSA and were stored
672 on ice until recovery.

673

674 **Recovery and plasmid extraction**

675 Following sorting, yeast were pelleted by spinning at 3,000xg for 10 min at 4°C. Supernatant was carefully
676 removed by pipette, and the resulting pellet was resuspended in 4 mL SDCAA and transferred to a glass
677 culture tube. A small amount of this resuspension (targeting 200-500 cells, based on sorting counts) was
678 plated on SDCAA-agar and YPD-agar to quantify recovery efficiency and plasmid loss. Cultures were
679 then rocked at 30°C until reaching OD600 = 0.8-2.

680

681 After reaching the target OD600, 1.5 mL yeast culture was pelleted and frozen at -80°C for at least an
682 hour. Plasmid was then extracted using the Zymo Yeast Plasmid Miniprep II kit (Zymo Research #D2004)
683 following the manufacturer's instructions, except for the following changes: 5 µL zymolyase was used per
684 sample, zymolyase incubations were 2-3 hours, precipitate following neutralization was removed by
685 centrifugation at 21,000xg for 10 minutes, columns were washed using 650 µL wash buffer and dried by
686 spinning at 16,000xg for 3 minutes, and plasmid was eluted in 15 µL elution buffer.

687

688 **Sequencing library preparation**

689 ScFv amplicon sequencing libraries were then prepared by a two-step PCR as previously described⁸⁶.
690 The first PCR appended unique molecular identifiers (UMI), sample-specific inline indices, and a partial
691 Illumina adapter to the scFv sequence, and was performed for 5 cycles to minimize PCR amplification
692 bias. The second PCR appended the remainder of the Illumina adapter and sample-specific Illumina i5
693 and i7 indices, and was performed for 35 cycles to produce a sufficient amount of each amplicon library
694 (primer sequences in Supplementary File 4). The first PCR used 5 µL plasmid DNA as template for a 20
695 µL reaction using Q5 polymerase according to the manufacturer's instructions with the following cycling
696 program: 1. 60 s at 98°C, 2. 10 s at 98°C, 3. 30 s at 67°C, 4. 60 s at 72°C, 5. GOTO 2, 4x, 6. 60 s at
697 72°C. The product from PCR 1 was then brought up to 40 µL with MBG water, purified using Aline beads
698 at a ratio of 1.2X, and eluted in 35 µL elution buffer. 33 µL of this elution was used as template for the
699 second PCR, which was a 50 µL reaction using Kapa polymerase (Kapa Biosystems, Wilmington, MA,
700 #K2502) per the manufacturer's instructions and the following cycling program: 1. 30 s at 98°C, 2. 20 s
701 at 98°C, 3. 30 s at 62°C, 4. 30 s at 72°C, 5. GOTO 2, 34x, 6. 300 s at 72°C. The resulting amplicons were
702 purified using Aline beads at a ratio of 0.85X and DNA concentration was determined using a fluorescent
703 DNA-binding dye (Biotum, Fremont, CA, #31068) per the manufacturer's instructions. Amplicons were
704 then pooled amongst the four bins for each concentration, based on the number of cells sorted into each
705 gate, and then equimolar amounts of the resulting pools were combined to make the final pooled library.

706 Prior to sequencing, the pool concentration was determined by Qubit and the size verified by Tapestation
707 HS DNA 5000 and 1000. The pool was then sequenced on a NovaSeq SP (2x250 paired-end reads) with
708 10% PhiX spike-in; 2-4 curves were loaded onto a single flow cell to sequence each variant at at least
709 100X coverage.

710

711 **Sequencing data processing**

712 Demultiplexed sequencing reads were parsed using a Snakemake pipeline as previously described⁸⁷
713 (see github.com/amphilli/CH65-comblib for parameters). Briefly, UMI, inline indices, and genotypes were
714 extracted from each read using Regex⁸⁸. Reads with incorrectly paired inline indices or unexpected
715 mutations at the CH65 mutation sites were discarded. In all other regions of the read, all reads exceeding
716 a 10% error rate were discarded. Following this filtering, reads were deduplicated by UMI to generate
717 unique counts files for each sample.

718

719 **Tite-Seq K_D inference**

720

721 **Mean-bin approach**

722 To fit the dissociation constant (K_D) for each variant in the library, we followed the same method as
723 previously described⁵. Briefly, we use the sequencing counts and flow cytometry data to infer the mean
724 log-fluorescence of each genotype s at each concentration c :

725

$$726 \quad \bar{F}_{s,c} = \sum_b F_{b,c} p_{b,s|c},$$

727

728 Where $F_{b,c}$ is the mean log-fluorescence of bin b at concentration c , and $p_{b,s|c}$ is the proportion of cells
729 with genotype s sorted into bin b at concentration c , and is given by:

730

$$731 \quad p_{b,s|c} = \frac{\frac{R_{b,s,c}}{\sum_s R_{b,s,c}} C_{b,c}}{\sum_b \left(\frac{R_{b,s,c}}{\sum_s R_{b,s,c}} C_{b,c} \right)}$$

732

733 Where $R_{b,s,c}$ is the number of reads with genotype s found in bin b at concentration c , and $c_{b,c}$ is the
734 number of cells sorted into bin b at concentration c .

735

736 Uncertainty is then propagated in these mean bin estimate as:

737

$$738 \quad \delta \bar{F}_{s,c} = \sqrt{\sum_b (\delta F_{b,c}^2 p_{b,s|c}^2 + F_{b,c}^2 \delta p_{b,s|c}^2)}$$

739

740 Where $\delta F_{b,c}$ is the standard deviation of log-fluorescence for cells sorted into bin b at concentration c .
741 This is approximated by $\sigma F_{b,c}$ and the error in $p_{b,s|c}$ results from sampling error, which is approximated as
742 a Poisson process at sufficient sequencing coverage, yielding:

743

$$744 \quad \delta p_{b,s|c} = \frac{p_{b,s|c}}{\sqrt{R_{b,s,c}}}.$$

745

746 The dissociation constant, $K_{D,s}$, was inferred for each genotype by fitting the logarithm of the Hill
747 function to the mean log-fluorescence:

748

$$\bar{F}_{s,c} = \log_{10} \left(\frac{c}{c + K_{D,s}} A_s + B_s \right)$$

749

750

751 Where A_s is the increase in fluorescence at antigen saturation and B_s is the background fluorescence in
752 the absence of antigen. The fit was performed using the Python package `scipy.optimize.curve_fit`
753 function, using the following boundary conditions: A_s ($10^2 - 10^6$), B_s ($1 - 10^5$), $K_{D,s}$ ($10^{-14} - 10^{-5}$).

754

755 **Data quality and filtering**

756 Following the $K_{D,s}$ inference, non-binding sequences with $K_{D,s} < 6$ or $A_s - B_s < 1$ were pinned to the titration
757 boundary with $-\log K_{D,s} = 6$. Subsequently, $K_{D,s}$ values resulting from poor fits ($r^2 < 0.8$, $\sigma > 1$) were
758 removed from the dataset, $K_{D,s}$ were averaged across biological replicates, and $K_{D,s}$ with large SEM ($>$
759 0.5-log units) were excluded from subsequent analyses. This filtering retained 65,530, 64,142, and
760 65,389 genotypes for the MA90, G189E, and SI06 Tite-Seq experiments, respectively (**Figure 1–source**
761 **data 1**).

762

763 **Expression data**

764 Sequencing reads corresponding to the expression sort were handled identically to those from the HA
765 binding sort, and the mean log-fluorescence was inferred as detailed above. Day-to-day variation in
766 fluorophore labeling and detection were accounted for by normalizing mean log-fluorescence values by
767 the average mean log-fluorescence of the corresponding replicate (**Figure 1–source data 1**).

768

769 **Force-directed layouts**

770 To reduce the dimensionality of the sequence-affinity landscape, we implemented a force-directed layout,
771 as previously described⁵. In these graphs, each variant sequence is represented by a node, and variants
772 related by a single mutation are connected by an edge. Edge weights between nodes s and t are weighted
773 by the change in binding affinity resulting from the corresponding mutation:

774

775

$$w_{s,t} = \frac{1}{0.01 + |\log_{10} K_{D,s} - \log_{10} K_{D,t}|}$$

776

777 To construct the force-directed layout, we use $K_{D,s}$ to MA90 to compute the weights. If a mutation from
778 sequence s to t does not impact $K_{D,s}$, those nodes will be close together, and vice versa. The layout
779 coordinates for each variant were obtained using the Python package iGraph function `layout_drl`, and
780 each node is associated with the corresponding $K_{D,s}$ to SI06 and G189E, as well as the mean expression.
781 An interactive form of this graph is available as an online data browser here: [https://ch65-ma90-](https://ch65-ma90-browser.netlify.app/)
782 [browser.netlify.app/](https://ch65-ma90-browser.netlify.app/).

783

784 **Epistasis Analysis**

785

786 **Linear interaction models**

787 We infer epistatic coefficients as previously described⁵. Briefly, we implement linear models to infer
788 specific mutational effects and interactions that sum to the observed log-transformed binding affinities, -

789 $\log(K_{D,s})$, which are proportional to free energy changes and hence expected to be additive^{62,63}. This
790 additive model is given by:

791

$$792 \quad y_s = \beta_0 + \sum_{i=1}^L \beta_i x_{i,s} + \varepsilon$$

793

794 Where L is the number of mutations in CH65 (i.e. 16), β_0 is an intercept, β_i is the effect of mutation at site
795 i , $x_{i,s}$ is the genotype of variant s at site i , and ε represents independently and identically distributed errors.
796 Our general epistatic model is thus given by:

797

$$798 \quad y_s = \beta_0 + \sum_i \beta_i x_{i,s} + \sum_{i<j} \beta_{ij} x_{i,s} x_{j,s} + \sum_{i<j<k} \beta_{ijk} x_{i,s} x_{j,s} x_{k,s} + \dots + \varepsilon$$

799

800 Where β_{ij} are second-order interaction coefficients between sites i and j , β_{ijk} are third-order interaction
801 coefficients between sites i , j , and k , and so on, up to a specified maximum order of interaction.

802

803 We infer these coefficients in both the biochemical and statistical bases^{5,89}, which are equivalent
804 frameworks related by a linear transformation. For ease of interpretation, we report coefficients inferred
805 using the biochemical model in the Main text and figures, as these coefficients can be interpreted as
806 mutational effects and interactions relative to the UCA860 sequence. We report coefficients inferred using
807 the statistical model in the Figure supplements, and these mutational effects and coefficients can be
808 interpreted as relative to the average of the dataset.

809

810 For both the biochemical and statistical models, we take a conservative approach to estimating higher-
811 order epistasis. To this end, we truncate the model above some maximal order n and fit the resulting
812 model, beginning with $n = 1$ and proceeding with higher n until the optimal performing model has been
813 identified. We evaluate performance using a cross-validation approach. For each of ten folds, we use
814 90% of the data to train the model and evaluate the model using the prediction performance (R^2) on the
815 remaining 10%. We then average performance across the ten folds, select the order that maximizes the
816 prediction performance, and retrain the entire dataset on a model truncated at this optimal order. This
817 inference yields models with p coefficients, and we find that for each antigen $p < N$ by an order of
818 magnitude, where N is the number of data points, giving us confidence that we are not overfitting the
819 data.

820

821 Practically, we perform this inference using the Python package stats models using ordinary least
822 squares regression. This yields the coefficient values and associated standard errors and p -values
823 (**Figure 3–source data 1**); coefficients with Bonferroni-corrected p -value < 0.05 are considered
824 significant and are plotted in **Figure 3** and **Figure 3–figure supplement 2**. For the SI06 data, we exclude
825 N52H from the epistasis inference and perform the analysis on the remaining 15 mutations, as $> 90\%$
826 of sequences with any detectable binding affinity include mutation N52H and thus we do not have power to
827 infer the effect of this mutation. In the statistical epistasis inference, the coefficients at different orders
828 are statistically independent and so we partition the variance explained by the model for each interaction
829 order (**Figure 3–figure supplement 2**)

830
831

832 **Structural analysis of epistasis**

833 To examine the structural context of the linear and pairwise coefficients from the biochemical epistasis
834 model, we performed two analyses using the co-crystal structure of CH65 with full-length Influenza
835 A/Solomon Islands/3/2006 HA (PDB 5UGY³). First, we used ChimeraX⁹⁰ to compute the buried surface
836 area between each mutation in CH65 and HA, using the *measure_buriedarea* function and the default
837 *probeRadius* of 1.4 angstroms. This area is plotted as the 'HA contact surface area' in **Figure 3**. We
838 perform the same computation between each mutation in CH65 and the HCDR3, and plot this as the
839 'CDR3 contact surface area' in **Figure 3**. Second, we used PyMol (The PyMOL Molecular Graphics
840 System, Version 2.0 Schrödinger, LLC) to compute the distance between alpha-carbons, and plot this as
841 a function of the pairwise interaction terms in **Figure 3—figure supplement 1**.

842

843 **Pathway Analysis**

844

845 **Selection models**

846 To assess the likelihood of mutational pathways from UCA860 to CH65, we assume a moderate selection
847 model in the weak-mutation strong-selection regime as previously described⁵. Briefly, in this model,
848 mutations fix independently of each other, and mutations are favored if they improve affinity, though both
849 neutral and deleterious mutations are allowed. We use this model to compute the fixation probability of a
850 mutation from sequence s to t^{θ} . This fixation probability is then used to compute the transition probability
851 of the corresponding mutational step:

852

$$853 \quad p_{step}(\sigma, N) = \frac{1 - e^{-\sigma}}{1 - e^{-N\sigma}}$$

854

855 We define the selection coefficient σ to be proportional to the difference in $-\log K_D$ for a particular antigen
856 between sequences s and t :

857

$$858 \quad \sigma = \gamma \Delta_{s,t}^{ag} = \gamma(-\log_{10} K_{D,t}^{ag} - (-\log_{10} K_{D,s}^{ag}))$$

859

860 Where N is the effective population size and γ corresponds to the strength of selection. For the moderate
861 selection model applied here, we use $N = 1000$ and $\gamma = 1$. Additionally, to compute the total number of
862 mutational paths that improve in affinity at each step, we use $N \rightarrow \text{infinity}$ and $\gamma \rightarrow \text{infinity}$ such that $p_{step} =$
863 1 if the mutation improves affinity and $p_{step} = 0$ otherwise. These fixation probabilities are then used to
864 compute the transition probability for all sequences s, t over all antigens ag :

865

$$866 \quad P_{s,t}^{ag} = \begin{cases} p_{step}(\Delta_{s,t}^{ag}, \gamma, N), & \text{if } t \text{ has one more mutation than } s \\ 0, & \text{otherwise} \end{cases}$$

867

868 **Antigen selection scenario likelihood and mutation probabilities**

869 The transition probabilities described above were used to compute the total probability for a set of
870 possible antigen selection scenarios, and for select antigen selection scenarios, the probability of each
871 mutation occurring at a specific order (**Figure 5**). This was performed as previously described⁵, where
872 the probabilities $P_{s,t}^{ag}$ are stored as sparse transition matrices P^{ag} of dimension $2^N \times 2^N$ for each antigen,
873 where entries are nonzero when sequence t has one more mutation than sequence s . To evaluate the
874 total probability for a given antigen selection scenario, we compute the matrix product for all mutational
875 steps i under a specific sequence of antigen selection contexts ag_1, \dots, ag_L :

876

877

$$P_{tot} = \sum_{\text{paths}} \left(\prod_{\text{steps}} P_{step} \right) = \left[\prod_{i=1}^L P^{agi} \right]_{s_g, s_s}$$

878

879 Where $[.]_{s,s'}$ represents the matrix element in the row corresponding to genotype s and the column
 880 corresponding to genotype s' . Notably, transition probabilities are not normalized at each step. Thus,
 881 many pathways will not reach the somatic CH65 sequence and the likelihood assesses the probability of
 882 reaching the CH65 somatic sequence.

883

884 Here, we consider three classes of antigen selection scenarios. The simplest is a single-antigen selection
 885 scenario, in which all steps i use the same antigen. Second, we consider selection scenarios where steps
 886 can use different antigens in a non-repetitive manner. Finally, we consider a scenario that approximates
 887 exposure to a mixture of antigens^{66,73,92}, in which an antigen is drawn at random for each mutational step
 888 i . We then calculate P_{tot} for 1000 randomly drawn scenarios, report the average log probability, and
 889 illustrate mutational paths and orders for a scenario near the median probability from the 1000 draws.
 890 For all antigen selection scenarios, the error of P_{tot} is estimated by resampling the binding affinity from a
 891 normal distribution corresponding to its value and standard deviation. We perform this bootstrapping over
 892 ten iterations and report P_{tot} as the average.

893

894 To identify the most likely paths under a given selection scenario (as plotted in **Figure 5B**), we construct
 895 a directed graph, where each sequence s is a node, and edges connect nodes s and t that are separated
 896 by one mutation. The edge weights are calculated from the transition probability, $w_{s \rightarrow t} =$
 897 $-\log(P_{s,t}^{ag} + \epsilon)$. In this framework, we can use the *shortest_simple_paths* function in Python package
 898 *networkx*⁹³ to compute the most likely paths.

899

900 To calculate the probability that a mutation at site m happened at a specific step j , we normalize the
 901 transition matrix (i.e. all paths must reach the somatic CH65 sequence) for a given antigen selection
 902 context:

903

$$\tilde{P}_{s,t}^{ag} = P_{s,t}^{ag} \times \left(\sum_t P_{s,t}^{ag} \right)^{-1}$$

904

905 For $P_{s,t}^{ag} \neq 0$ and 0 otherwise. The total relative probability for that site mutating at a specific step under
 906 an antigen exposure scenario is given by:

907

908

$$P_{j,\alpha} = \left[\left(\prod_{i=1}^{j-1} \tilde{P}^{agi} \right) \cdot \tilde{P}_{\alpha}^{agj} \cdot \left(\prod_{i=j+1}^L \tilde{P}^{agi} \right) \right]_{s_g, s_s}$$

909

910 Finally, to determine the total probability of each variant (**Figure 5–Figure supplement 2**), which is given
 911 by the sum of the probabilities of all paths passing through that variant in a specific antigen selection
 912 scenario:

913

914

$$P_s = \left(\left[\prod_{i=1}^j \bar{p}^{agi} \right]_{s_g, s} \right) \cdot \left(\left[\prod_{i=j+1}^L \bar{p}^{agi} \right]_{s, s_s} \right)$$

915

916 Where j is the number of somatic mutations in variant s , the first term is the probability of reaching
917 sequence s at mutational step j , and the second term is the probability of reaching the CH65 sequence
918 after passing through sequence s . We perform an additional normalization, $P'_s = P_s \times n_j$, so that variants
919 with different numbers of mutations can be compared. P'_s is thus the probability of a specific variant in the
920 selective model compared to a neutral model (e.g. sequences with $\log(P'_s) > 0$ are favored).

921

922 **Isogenic K_D measurements**

923

924 To validate K_D measurements made using Tite-Seq, we generated isogenic yeast strains encoding select
925 variants in the CH65 scFv library and measured their affinity to HA using analytical flow cytometry. These
926 variants were constructed by the same Golden Gate strategy used above for the library, but by pooling
927 one version of each fragment rather than all versions of each fragment. The assembled plasmid was
928 sequence-verified via Sanger, transformed into the EBY100 yeast strain, plated on SDCAA-agar, and
929 incubated at 30°C for 48 h. Single colonies were then restructured onto SDCAA-agar and grown for an
930 additional 48 h at 30°C for further selection. These restructured colonies were verified to contain the scFv
931 plasmid by colony PCR. Verified colonies were then grown in 5 mL SDCAA with rotation at 30°C for 24h;
932 strains were stored by freezing saturated cultures with 5% glycerol at -80°C.

933

934 To measure K_D , yeast strains were thawed and scFv were induced, incubated with HA antigen, and
935 labeled with fluorophores as described above for the Tite-Seq assay, except yeast cell and antigen
936 volumes were scaled down by a factor of 10. Yeast cell FITC and R-PE fluorescence intensity were then
937 assayed on a BD LSR Fortessa equipped with four lasers (440, 488, 561, and 633 nm), sampling at least
938 10,000 events per concentration. The equilibrium dissociation constant, K_D , were then inferred for each
939 variant s by fitting the logarithm of a Hill function to the mean log R-PE fluorescence for the scFv-
940 expression (FITC-positive) single yeast cells:

941

$$942 \text{ mean log fluorescence} = \log_{10} \left(A_s \frac{c}{c + K_{D,s}} + B_s \right)$$

943

944

945 Where c is the molarity of antigen, A_s is the increase in fluorescence due to saturation with antigen and
946 B_s is the background fluorescence. All isogenic K_D measurements were made in 2-3 biological replicates
947 (**Figure 1–source data 2; Figure 1–figure supplement 3**).

948

949 **Fab structural characterization**

950

951 **Fab production and purification**

952 Antigen binding fragments were cloned and produced in Expi293F cells as above, except the variable
953 heavy chain was cloned into a pVRC expression vector containing the CH1 domain followed by a HRV
954 3C cleavage site and a 6X His tag. Fabs were purified by cobalt chromatography (Takara) and further
955 purified over an S200 column on an AKTA pure (Cytiva). To the purified Fabs, 1.2 μ L HRV 3C protease
956 (Thermo Scientific, #88947) per 200 μ g of Fab was added and incubated overnight at 4°C on a roller.

957 The next day, the cleaved Fab was passed over cobalt resin and purified again over an S200 column in
958 10 mM Tris HCl, 150 mM NaCl, pH 7.5. The resulting Fabs were concentrated to ~15 mg/mL prior to
959 crystallization.

960

961 **Fab crystallization**

962 Fabs were crystallized by the hanging drop method. Crystals of unbound UCA Fab with the Y35N (LC)
963 mutation and unbound I-2 Fab with H35N (HC) and Y35N (LC) mutations were grown over solutions of
964 0.1 M succinic acid (pH 7), 0.1 M bicine (pH 8.5), and 30% polyethylene glycol monomethyl ether 550 or
965 0.8 M lithium sulfate monohydrate, 0.1 M sodium acetate trihydrate (pH 4), and 4% polyethylene glycol
966 200 (Hampton Research, #HR2-084), respectively, in a 96-well plate (Greiner, #655101) with ViewDrop
967 II plate seals (sptlabtech, #4150-05600). Crystals were apparent after ~5-7 days. Then, 1 μ L of 12% (+/-)
968)-2-Methyl-2,4-pentanediol (MPD) in the corresponding solution was added for cryoprotection. The
969 crystals were then harvested and flash-cooled in liquid nitrogen.

970

971 **Fab structure determination**

972 X-ray diffraction data was collected at the Advanced Photon Source using beam line 24-ID-E. Diffraction
973 data was processed using XDSGUI ([https://strucbio.biologie.uni-
974 konstanz.de/xdswiki/index.php/XDSGUI](https://strucbio.biologie.uni-konstanz.de/xdswiki/index.php/XDSGUI)). Both Fabs reported here were solved by molecular
975 replacement using PHASER in the PHENIX-MR GUI^{94,95} by searching with the UCA Fab (PDB: 4HK0)⁴
976 with the HCDR3 deleted and separated into the VH, VL, CH, and CL domains. Refinement was performed
977 in PHENIX⁹⁴ by refining the coordinates and B factors before model building (i.e., the HCDR3) in COOT⁹⁶.
978 Additional placement of waters and Translation Libration Screw (TLS) refinement followed. The UCA with
979 Y35N Fab showed density for the HCDR3, which was built, but this loop exhibited large B factors (**Figure
980 4—figure supplement 1**). The I-2 with H35N and Y35N Fab showed no clear density for the HCDR3 or
981 the LCDR2 so these were removed from the structure. The resulting structures were validated using
982 MolProbity⁹⁷ prior to deposition at the Protein Data Bank (8EK6 and 8EKH).

983

984

985 **Antibody-antigen binding kinetics measurements**

986

987 Kinetics measurements were acquired on an Octet RED96e (Sartorius). To mimic the interaction between
988 yeast-displayed scFv and trimeric HA, IgG was loaded onto Anti-Human Fc Capture (AHC) biosensors
989 (Sartorius, #18-5060). To reduce the avidity effect, IgGs were loaded to a density of ~0.1 nm using a
990 solution of 10 nM of IgG. All binding measurements were obtained in “kinetics” buffer: PBS supplemented
991 with 0.1% BSA and 0.01% Tween20. Binding measurements were acquired as follows with shaking at
992 1000 rpm – Baseline: 60s; Loading: 30s with threshold at 0.1 nm; Baseline: 60s; Association: 360s;
993 Dissociation: 600s. Tips were regenerated a maximum of four times by alternating between 10 mM
994 Glycine (pH 1.7) and kinetics buffer three times with 10s in each buffer. Kinetics measurements were
995 obtained at four temperatures for each antibody: 20°C, 25°C, 30°C, and 35°C. Kinetics measurements
996 for the UCA, I-2, and CH65 were also acquired at 40°C. Prior to each measurement, the plate was allowed
997 to equilibrate to the set temperature for 20 minutes. Each full-length, trimeric HA (MA90, MA90-G189E,
998 and SI06) was assayed at six concentrations: 500, 250, 125, 62.5, 31.25, and 15.625 nM. For each
999 antibody against each HA, antibody assayed with buffer only was used as a reference for subtraction.
1000 Additionally, each run contained an irrelevant IgG (CR3022) at the highest HA concentration (500 nM) to
1001 detect any non-specific interaction, which was at background level. To account for the multivalency of
1002 the analyte (trimeric HA), the bivalent analyte model was used for global curve fitting in the Sartorius Data
1003 Analysis HT software version 12.0.2.59.

1004 **Acknowledgements**

1005 We thank Zach Niziolek for assistance with flow cytometry and members of the Desai lab for helpful
1006 discussions. We thank Jesse Bloom for providing the plasmids required to generate recombinant
1007 influenza viruses and Nicholas Heaton for sharing influenza virus-related protocols. A.M.P. acknowledges
1008 support from the Howard Hughes Medical Institute Hanna H. Gray Postdoctoral Fellowship, T.D.
1009 acknowledges support from the Human Frontier Science Program Postdoctoral Fellowship, A.G.S.
1010 acknowledges support for NIH grants R01AI146779 and P01AI89618-A1, M.M.D. acknowledges support
1011 from the NSF-Simons Center for Mathematical and Statistical Analysis of Biology at Harvard University,
1012 supported by NSF grant no. DMS-1764269, and the Harvard FAS Quantitative Biology Initiative, grant
1013 DEB-1655960 from the NSF and grant GM104239 from the NIH. Computational work was performed on
1014 the FASRC Cannon cluster supported by the FAS Division of Science Research Computing Group at
1015 Harvard University. We thank the beamline staff at NE-CAT for help with data collection; this work used
1016 NE-CAT beamlines (GM124165), a Pilatus detector (RR029205), an Eiger detector (OD021527) at the
1017 APS (DE-AC02-06CH11357).

1018

1019 **Author Contributions**

1020 Conceptualization: A.M.P., D.P.M., A.G.S, and M.M.D. Methodology: A.M.P., D.P.M., C.B., and T.D.
1021 Experiments: A.M.P., D.P.M., and C.B. Validation: A.M.P., D.P.M., and C.B. Data analysis: A.M.P.,
1022 D.P.M., C.B., and T.D. Supervision: A.M.P., A.G.S., and M.M.D. Funding acquisition: A.G.S. and M.M.D.
1023 Writing—original draft: A.M.P. and D.P.M. All the authors reviewed and edited the manuscript.

1024

1025 **Competing Interests**

1026 A.M.P. and M.M.D. have or have recently consulted for Leyden Labs. The other authors declare no
1027 competing financial interests.

1028

1029 **Materials and Correspondence**

1030 Correspondence and requests for materials should be addressed to M.M.D. (mdesai@oeb.harvard.edu).

1031

1032 **Data Availability**

1033 Data and code used for this study are available at <https://github.com/amphilli/CH65-comblib>. Antibody
1034 affinity and expression data are also available in an interactive data browser at [https://ch65-si06-
1035 browser.netlify.app/](https://ch65-si06-browser.netlify.app/). FASTQ files from high-throughput sequencing will be deposited in the NCBI
1036 BioProject database upon publication. X-ray crystal structures of the Fabs reported here are available at
1037 the Protein Data Bank (8EK6 and 8EKH).

1038

1039

1040 **References**

1041

1042 1 Corti, D., Cameroni, E., Guarino, B., Kallewaard, N. L., Zhu, Q. & Lanzavecchia, A. Tackling
1043 influenza with broadly neutralizing antibodies. *Curr. Opin. Virol.* **24**, 60-69 (2017).

1044 2 Sangesland, M. & Lingwood, D. Antibody focusing to conserved sites of vulnerability: The
1045 immunological pathways for 'universal' Influenza vaccines. *Vaccines* **9**, 125 (2021).

1046 3 Whittle, J. R. R., Zhang, R., Khurana, S., King Lisa, R., Manischewitz, J., Golding, H., Dormitzer
1047 Philip, R., Haynes Barton, F., Walter Emmanuel, B., Moody, M. A., Kepler Thomas, B., Liao, H.-
1048 X. & Harrison Stephen, C. Broadly neutralizing human antibody that recognizes the receptor-
1049 binding pocket of influenza virus hemagglutinin. *Proc. Natl. Acad. Sci. USA* **108**, 14216-14221
1050 (2011).

1051 4 Schmidt, A. G., Xu, H., Khan, A. R., O'Donnell, T., Khurana, S., King, L. R., Manischewitz, J.,
1052 Golding, H., Suphaphiphat, P. & Carfi, A. Preconfiguration of the antigen-binding site during
1053 affinity maturation of a broadly neutralizing influenza virus antibody. *Proc. Natl. Acad. Sci. USA*
1054 **110**, 264-269 (2013).

1055 5 Phillips, A. M., Lawrence, K. R., Moulana, A., Dupic, T., Chang, J., Johnson, M. S., Cvijovic, I.,
1056 Mora, T., Walczak, A. M. & Desai, M. M. Binding affinity landscapes constrain the evolution of
1057 broadly neutralizing anti-influenza antibodies. *Elife* **10**, e71393 (2021).

1058 6 Kubo, M. & Miyauchi, K. Breadth of antibody responses during influenza virus infection and
1059 vaccination. *Trends in Immunol.* **41**, 394-405 (2020).

1060 7 Angeletti, D. & Yewdell, J. W. Is it possible to develop a "universal" influenza virus vaccine?
1061 Outflanking antibody immunodominance on the road to universal influenza vaccination. *Cold*
1062 *Spring Harb. Perspect. Biol.* **10**, a028852 (2018).

1063 8 Neher, R. A. & Bedford, T. Nextflu: real-time tracking of seasonal influenza virus evolution in
1064 humans. *Bioinform.* **31**, 3546-3548 (2015).

1065 9 Dugan, H. L., Guthmiller, J. J., Arevalo, P., Huang, M., Chen, Y.-Q., Neu, K. E., Henry, C., Zheng,
1066 N.-Y., Lan, L. Y.-L., Tepora, M. E., Stovicek, O., Bitar, D., Palm, A.-K. E., Stamper, C. T.,
1067 Changrob, S., Utset, H. A., Coughlan, L., Krammer, F., Cobey, S. & Wilson, P. C. Preexisting
1068 immunity shapes distinct antibody landscapes after influenza virus infection and vaccination in
1069 humans. *Sci. Transl. Med.* **12**, eabd3601 (2020).

1070 10 Throsby, M., van den Brink, E., Jongeneelen, M., Poon, L. L., Alard, P., Cornelissen, L., Bakker,
1071 A., Cox, F., van Deventer, E., Guan, Y., Cinatl, J., ter Meulen, J., Lasters, I., Carsetti, R., Peiris,
1072 M., de Kruif, J. & Goudsmit, J. Heterosubtypic neutralizing monoclonal antibodies cross-protective
1073 against H5N1 and H1N1 recovered from human IgM+ memory B cells. *PLoS One* **3**, e3942
1074 (2008).

1075 11 Corti, D., Voss, J., Gamblin, S. J., Codoni, G., Macagno, A., Jarrossay, D., Vachieri, S. G., Pinna,
1076 D., Minola, A., Vanzetta, F., Silacci, C., Fernandez-Rodriguez, B. M., Agatic, G., Bianchi, S.,
1077 Giacchetto-Sasselli, I., Calder, L., Sallusto, F., Collins, P., Haire, L. F., Temperton, N., Langedijk,
1078 J. P., Skehel, J. J. & Lanzavecchia, A. A neutralizing antibody selected from plasma cells that
1079 binds to group 1 and group 2 influenza A hemagglutinins. *Science* **333**, 850-856 (2011).

1080 12 Dreyfus, C., Laursen, N. S., Kwaks, T., Zuijdgeest, D., Khayat, R., Ekiert, D. C., Lee, J. H.,
1081 Metlagel, Z., Bujny, M. V., Jongeneelen, M., van der Vlugt, R., Lamrani, M., Korse, H. J. W. M.,
1082 Geelen, E., Sahin, Ö., Sieuwerts, M., Brakenhoff, J. P. J., Vogels, R., Li, O. T. W., Poon, L. L. M.,

- 1083 Peiris, M., Koudstaal, W., Ward, A. B., Wilson, I. A., Goudsmit, J. & Friesen, R. H. E. Highly
1084 conserved protective epitopes on Influenza B viruses. *Science* **337**, 1343-1348 (2012).
- 1085 13 Ekiert, D. C., Bhabha, G., Elsliger, M. A., Friesen, R. H., Jongeneelen, M., Throsby, M., Goudsmit,
1086 J. & Wilson, I. A. Antibody recognition of a highly conserved influenza virus epitope. *Science* **324**,
1087 246-251 (2009).
- 1088 14 Raymond, D. D., Bajic, G., Ferdman, J., Suphaphiphat, P., Settembre, E. C., Moody, M. A.,
1089 Schmidt, A. G. & Harrison, S. C. Conserved epitope on influenza-virus hemagglutinin head
1090 defined by a vaccine-induced antibody. *Proc. Natl. Acad. Sci. USA* **115**, 168-173 (2018).
- 1091 15 Guthmiller, J. J., Han, J., Utset, H. A., Li, L., Lan, L. Y.-L., Henry, C., Stamper, C. T., McMahon,
1092 M., O'Dell, G. & Fernández-Quintero, M. L. Broadly neutralizing antibodies target a
1093 haemagglutinin anchor epitope. *Nature* **602**, 314-320 (2022).
- 1094 16 Jiang, N., He, J., Weinstein, J. A., Penland, L., Sasaki, S., He, X.-S., Dekker, C. L., Zheng, N.-Y.,
1095 Huang, M. & Sullivan, M. Lineage structure of the human antibody repertoire in response to
1096 influenza vaccination. *Sci. Transl. Med.* **5**, 171ra119 (2013).
- 1097 17 Horns, F., Vollmers, C., Dekker, C. L. & Quake, S. R. Signatures of selection in the human
1098 antibody repertoire: Selective sweeps, competing subclones, and neutral drift. *Proc. Natl. Acad.
1099 Sci. USA* **116**, 1261-1266 (2019).
- 1100 18 Wu, N. C., Grande, G., Turner, H. L., Ward, A. B., Xie, J., Lerner, R. A. & Wilson, I. A. In vitro
1101 evolution of an influenza broadly neutralizing antibody is modulated by hemagglutinin receptor
1102 specificity. *Nat. Comm.* **8**, 1-12 (2017).
- 1103 19 Bajic, G., van der Poel, C. E., Kuraoka, M., Schmidt, A. G., Carroll, M. C., Kelsoe, G. & Harrison,
1104 S. C. Autoreactivity profiles of influenza hemagglutinin broadly neutralizing antibodies. *Sci. Rep.*
1105 **9**, 1-9 (2019).
- 1106 20 Horns, F., Dekker, C. L. & Quake, S. R. Memory B Cell Activation, Broad Anti-influenza
1107 Antibodies, and Bystander Activation Revealed by Single-Cell Transcriptomics. *Cell Rep.* **30**, 905-
1108 913 (2020).
- 1109 21 Abbott, R. K., Lee, J. H., Menis, S., Skog, P., Rossi, M., Ota, T., Kulp, D. W., Bhullar, D.,
1110 Kalyuzhnyi, O. & Havenar-Daughton, C. Precursor frequency and affinity determine B cell
1111 competitive fitness in germinal centers, tested with germline-targeting HIV vaccine immunogens.
1112 *Immunity* **48**, 133-146. e136 (2018).
- 1113 22 Andrews, S. F., Huang, Y., Kaur, K., Popova, L. I., Ho, I. Y., Pauli, N. T., Henry Dunand, C. J.,
1114 Taylor, W. M., Lim, S., Huang, M., Qu, X., Lee, J. H., Salgado-Ferrer, M., Krammer, F., Palese,
1115 P., Wrammert, J., Ahmed, R. & Wilson, P. C. Immune history profoundly affects broadly protective
1116 B cell responses to influenza. *Sci. Transl. Med.* **7**, 316ra192 (2015).
- 1117 23 Starr, T. N., Picton, L. K. & Thornton, J. W. Alternative evolutionary histories in the sequence
1118 space of an ancient protein. *Nature* **549**, 409-413 (2017).
- 1119 24 Miton, C. & Tokuriki, N. How mutational epistasis impairs predictability in protein evolution and
1120 design. *Protein Sci.* **25**, 1260-1272 (2016).
- 1121 25 Bank, C., Hietpas, R. T., Jensen, J. D. & Bolon, D. N. A. A systematic survey of an intragenic
1122 epistatic landscape. *Mol. Biol. Evol.* **32**, 229-238 (2015).

- 1123 26 Phillips, A. M., Ponomarenko, A. I., Chen, K., Ashenberg, O., Miao, J., McHugh, S. M., Butty, V.
1124 L., Whittaker, C. A., Moore, C. L., Bloom, J. D., Lin, Y.-S. & Shoulders, M. D. Destabilized adaptive
1125 influenza variants critical for innate immune system escape are potentiated by host chaperones.
1126 *PLoS Biol.* **16**, e3000008 (2018).
- 1127 27 Weinreich, D. M., Delaney, N. F., Depristo, M. A. & Hartl, D. L. Darwinian evolution can follow
1128 only very few mutational paths to fitter proteins. *Science* **312**, 111-114 (2006).
- 1129 28 Gong, L. I., Suchard, M. A. & Bloom, J. D. Stability-mediated epistasis constrains the evolution of
1130 an influenza protein. *eLife* **2**, e00631 (2013).
- 1131 29 Sailer, Z. R. & Harms, M. J. High-order epistasis shapes evolutionary trajectories. *PLoS Comput.*
1132 *Biol.* **13**, e1005541 (2017).
- 1133 30 Adams, R. M., Mora, T., Walczak, A. M. & Kinney, J. B. Measuring the sequence-affinity
1134 landscape of antibodies with massively parallel titration curves. *Elife* **5**, e23156 (2016).
- 1135 31 Forsyth, C. M., Juan, V., Akamatsu, Y., DuBridge, R. B., Doan, M., Ivanov, A. V., Ma, Z., Polakoff,
1136 D., Razo, J. & Wilson, K. Deep mutational scanning of an antibody against epidermal growth
1137 factor receptor using mammalian cell display and massively parallel pyrosequencing. *MAbs* **5**,
1138 523-532 (2013).
- 1139 32 Li, D., Wang, L., Maziuk, B. F., Yao, X., Wolozin, B. & Cho, Y. K. Directed evolution of a picomolar-
1140 affinity, high-specificity antibody targeting phosphorylated tau. *J. Biol. Chem.* **293**, 12081-12094
1141 (2018).
- 1142 33 Amon, R., Rosenfeld, R., Perlmutter, S., Grant, O. C., Yehuda, S., Borenstein-Katz, A., Alcalay,
1143 R., Marshanski, T., Yu, H. & Diskin, R. Directed evolution of therapeutic antibodies targeting
1144 glycosylation in cancer. *Cancers* **12**, 2824 (2020).
- 1145 34 Bowers, P. M., Boyle, W. J. & Damoiseaux, R. in *Antibody Engineering: Methods and Protocols*
1146 (eds Damien Nevoltris & Patrick Chames) 479-489 (Springer New York, 2018).
- 1147 35 Vitorica, G. D. & Nussenzweig, M. C. Germinal centers. *Annu. Rev. Immunol.* **30**, 429-457 (2012).
- 1148 36 Smith, D. J., Lapedes, A. S., de Jong, J. C., Bestebroer, T. M., Rimmelzwaan, G. F., Osterhaus,
1149 A. D. M. E. & Fouchier, R. A. M. Mapping the antigenic and genetic evolution of Influenza virus.
1150 *Science* **305**, 371-376 (2004).
- 1151 37 Braden, B. C., Goldman, E. R., Mariuzza, R. A. & Poljak, R. J. Anatomy of an antibody molecule:
1152 structure, kinetics, thermodynamics and mutational studies of the antilysozyme antibody D1.3.
1153 *Immunol. Rev.* **163**, 45-57 (1998).
- 1154 38 Burks, E. A., Chen, G., Georgiou, G. & Iverson, B. L. In vitro scanning saturation mutagenesis of
1155 an antibody binding pocket. *Proc. Natl. Acad. Sci. USA* **94**, 412-417 (1997).
- 1156 39 Chen, Y., Wiesmann, C., Fuh, G., Li, B., Christinger, H. W., McKay, P., de Vos, A. M. & Lowman,
1157 H. B. Selection and analysis of an optimized anti-VEGF antibody: crystal structure of an affinity-
1158 matured Fab in complex with antigen. *J. Mol. Biol.* **293**, 865-881 (1999).
- 1159 40 Klein, C., Lammens, A., Schäfer, W., Georges, G., Schwaiger, M., Mössner, E., Hopfner, K. P.,
1160 Umaña, P. & Niederfellner, G. Epitope interactions of monoclonal antibodies targeting CD20 and
1161 their relationship to functional properties. *MAbs* **5**, 22-33 (2013).

- 1162 41 Corti, D. & Lanzavecchia, A. Broadly neutralizing antiviral antibodies. *Annu. Rev. Immunol.* **31**,
1163 705-742 (2013).
- 1164 42 Unniraman, S. & Schatz, D. G. Strand-biased spreading of mutations during somatic
1165 hypermutation. *Science* **317**, 1227-1230 (2007).
- 1166 43 Pappas, L., Foglierini, M., Piccoli, L., Kallewaard, N. L., Turrini, F., Silacci, C., Fernandez-
1167 Rodriguez, B., Agatic, G., Giacchetto-Sasselli, I., Pellicciotta, G., Sallusto, F., Zhu, Q., Vicenzi,
1168 E., Corti, D. & Lanzavecchia, A. Rapid development of broadly influenza neutralizing antibodies
1169 through redundant mutations. *Nature* **516**, 418-422 (2014).
- 1170 44 Adams, R. M., Kinney, J. B., Walczak, A. M. & Mora, T. Epistasis in a fitness landscape defined
1171 by antibody-antigen binding free energy. *Cell Syst.* **8**, 86-93 (2019).
- 1172 45 Yassine, H. M., McTamney, P. M., Boyington, J. C., Ruckwardt, T. J., Crank, M. C., Smatti, M. K.,
1173 Ledgerwood, J. E. & Graham, B. S. Use of hemagglutinin stem probes demonstrate prevalence
1174 of broadly reactive Group 1 Influenza antibodies in human sera. *Sci. Rep.* **8**, 8628 (2018).
- 1175 46 Wu, N. C., Thompson, A. J., Lee, J. M., Su, W., Arlian, B. M., Xie, J., Lerner, R. A., Yen, H.-L.,
1176 Bloom, J. D. & Wilson, I. A. Different genetic barriers for resistance to HA stem antibodies in
1177 influenza H3 and H1 viruses. *Science* **368**, 1335-1340 (2020).
- 1178 47 Ellebedy, A. H. Immunizing the immune: Can we overcome Influenza's most formidable
1179 challenge? *Vaccines* **6** (2018).
- 1180 48 Han, A., Czajkowski, L., Rosas, L. A., Cervantes-Medina, A., Xiao, Y., Gouzoulis, M., Lumbard,
1181 K., Hunsberger, S., Reed, S., Athota, R., Baus, H. A., Lwin, A., Sadoff, J., Taubenberger, J. K. &
1182 Memoli, M. J. Safety and efficacy of CR6261 in an influenza A H1N1 healthy human challenge
1183 model. *Clin. Infect. Dis.* **73**, e4260-e4268 (2021).
- 1184 49 Schmidt, A. G., Therkelsen, M. D., Stewart, S., Kepler, T. B., Liao, H. X., Moody, M. A., Haynes,
1185 B. F. & Harrison, S. C. Viral receptor-binding site antibodies with diverse germline origins. *Cell*
1186 **161**, 1026-1034 (2015).
- 1187 50 Lee, P. S., Ohshima, N., Stanfield, R. L., Yu, W., Iba, Y., Okuno, Y., Kurosawa, Y. & Wilson, I. A.
1188 Receptor mimicry by antibody F045-092 facilitates universal binding to the H3 subtype of
1189 influenza virus. *Nat. Comm.* **5**, 3614 (2014).
- 1190 51 Krause, J. C., Tsibane, T., Tumpey, T. M., Huffman, C. J., Basler, C. F. & Crowe, J. E., Jr. A
1191 broadly neutralizing human monoclonal antibody that recognizes a conserved, novel epitope on
1192 the globular head of the influenza H1N1 virus hemagglutinin. *J. Virol.* **85**, 10905-10908 (2011).
- 1193 52 Guthmiller, J. J., Utset, H. A. & Wilson, P. C. B cell responses against Influenza viruses: Short-
1194 lived humoral immunity against a life-long threat. *Viruses* **13**, 965 (2021).
- 1195 53 DiLillo, D. J., Tan, G. S., Palese, P. & Ravetch, J. V. Broadly neutralizing hemagglutinin stalk-
1196 specific antibodies require FcγR interactions for protection against influenza virus in vivo. *Nat.*
1197 *Med.* **20**, 143-151 (2014).
- 1198 54 Xu, H., Schmidt, A. G., O'Donnell, T., Therkelsen, M. D., Kepler, T. B., Moody, M. A., Haynes, B.
1199 F., Liao, H. X., Harrison, S. C. & Shaw, D. E. Key mutations stabilize antigen-binding conformation
1200 during affinity maturation of a broadly neutralizing influenza antibody lineage. *Proteins* **83**, 771-
1201 780 (2015).

- 1202 55 Schmidt, A. G., Do, K. T., McCarthy, K. R., Kepler, T. B., Liao, H.-X., Moody, M. A., Haynes,
1203 Barton F. & Harrison, Stephen C. Immunogenic stimulus for germline precursors of antibodies
1204 that engage the Influenza hemagglutinin receptor-binding site. *Cell Rep.* **13**, 2842-2850 (2015).
- 1205 56 Lingwood, D., McTamney, P. M., Yassine, H. M., Whittle, J. R., Guo, X., Boyington, J. C., Wei, C.
1206 J. & Nabel, G. J. Structural and genetic basis for development of broadly neutralizing influenza
1207 antibodies. *Nature* **489**, 566-570 (2012).
- 1208 57 Xiao, H., Guo, T., Yang, M., Qi, J., Huang, C., Hong, Y., Gu, J., Pang, X., Liu, W. J., Peng, R.,
1209 McCauley, J., Bi, Y., Li, S., Feng, J., Zhang, H., Zhang, X., Lu, X., Yan, J., Chen, L., Shi, Y., Chen,
1210 W. & Gao, G. F. Light chain modulates heavy chain conformation to change protection profile of
1211 monoclonal antibodies against influenza A viruses. *Cell Discov.* **5**, 21 (2019).
- 1212 58 Ekiert, D. C. & Wilson, I. A. Broadly neutralizing antibodies against influenza virus and prospects
1213 for universal therapies. *Curr. Opin. Virol.* **2**, 134-141 (2012).
- 1214 59 Boder, E. T. & Wittrup, K. D. Yeast surface display for screening combinatorial polypeptide
1215 libraries. *Nat. Biotech.* **15**, 553-557 (1997).
- 1216 60 Bedford, T., Suchard, M. A., Lemey, P., Dudas, G., Gregory, V., Hay, A. J., McCauley, J. W.,
1217 Russell, C. A., Smith, D. J. & Rambaut, A. Integrating influenza antigenic dynamics with molecular
1218 evolution. *Elife* **3**, e01914 (2014).
- 1219 61 Muecksch, F., Weisblum, Y., Barnes, C. O., Schmidt, F., Schaefer-Babajew, D., Wang, Z., JC, C.
1220 L., Flyak, A. I., DeLaitch, A. T., Huey-Tubman, K. E., Hou, S., Schiffer, C. A., Gaebler, C., Da
1221 Silva, J., Poston, D., Finkin, S., Cho, A., Cipolla, M., Oliveira, T. Y., Millard, K. G., Ramos, V.,
1222 Gazumyan, A., Rutkowska, M., Caskey, M., Nussenzweig, M. C., Bjorkman, P. J., Hatziioannou,
1223 T. & Bieniasz, P. D. Affinity maturation of SARS-CoV-2 neutralizing antibodies confers potency,
1224 breadth, and resilience to viral escape mutations. *Immunity* **54**, 1853-1868.e1857 (2021).
- 1225 62 Wells, J. A. Additivity of mutational effects in proteins. *Biochemistry* **29**, 8509-8517 (1990).
- 1226 63 Olson, C. A., Wu, N. C. & Sun, R. A comprehensive biophysical description of pairwise epistasis
1227 throughout an entire protein domain. *Curr. Biol.* **24**, 2643-2651 (2014).
- 1228 64 Lee, P. S., Arnell, A. J. & Wilson, I. A. Structure of the apo anti-influenza CH65 Fab. *Acta*
1229 *Crystallogr. F: Struct. Biol. Commun.* **71**, 145-148 (2015).
- 1230 65 Valley, C. C., Cembran, A., Perlmutter, J. D., Lewis, A. K., Labello, N. P., Gao, J. & Sachs, J. N.
1231 The methionine-aromatic motif plays a unique role in stabilizing protein structure. *J. Biol. Chem.*
1232 **287**, 34979-34991 (2012).
- 1233 66 Wang, S., Mata-Fink, J., Kriegsman, B., Hanson, M., Irvine, D. J., Eisen, H. N., Burton, D. R.,
1234 Wittrup, K. D., Kardar, M. & Chakraborty, A. K. Manipulating the selection forces during affinity
1235 maturation to generate cross-reactive HIV antibodies. *Cell* **160**, 785-797 (2015).
- 1236 67 Liao, H.-X., Lynch, R., Zhou, T., Gao, F., Alam, S. M., Boyd, S. D., Fire, A. Z., Roskin, K. M.,
1237 Schramm, C. A., Zhang, Z., Zhu, J., Shapiro, L., Becker, J., Benjamin, B., Blakesley, R., Bouffard,
1238 G., Brooks, S., Coleman, H., Dekhtyar, M., Gregory, M., Guan, X., Gupta, J., Han, J., Hargrove,
1239 A., Ho, S.-I., Johnson, T., Legaspi, R., Lovett, S., Maduro, Q., Masiello, C. *et al.* Co-evolution of
1240 a broadly neutralizing HIV-1 antibody and founder virus. *Nature* **496**, 469-476 (2013).

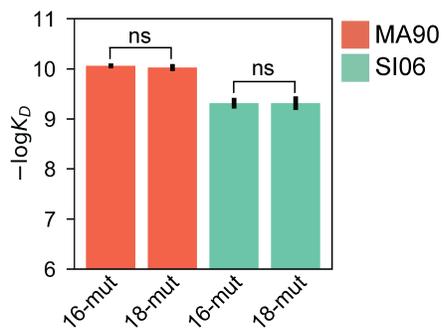
- 1241 68 Fera, D., Schmidt, A. G., Haynes, B. F., Gao, F., Liao, H. X., Kepler, T. B. & Harrison, S. C. Affinity
1242 maturation in an HIV broadly neutralizing B-cell lineage through reorientation of variable domains.
1243 *Proc. Natl. Acad. Sci. USA* **111**, 10275-10280 (2014).
- 1244 69 Ovchinnikov, V., Louveau, J. E., Barton, J. P., Karplus, M. & Chakraborty, A. K. Role of framework
1245 mutations and antibody flexibility in the evolution of broadly neutralizing antibodies. *Elife* **7**,
1246 e33038 (2018).
- 1247 70 McCarthy, K. R., Raymond, D. D., Do, K. T., Schmidt, A. G. & Harrison, S. C. Affinity maturation
1248 in a human humoral response to influenza hemagglutinin. *Proc. Natl. Acad. Sci. USA* **116**, 26745-
1249 26751 (2019).
- 1250 71 Turner, J. S., Zhou, J. Q., Han, J., Schmitz, A. J., Rizk, A. A., Alsoussi, W. B., Lei, T., Amor, M.,
1251 McIntire, K. M., Meade, P., Strohmeier, S., Brent, R. I., Richey, S. T., Haile, A., Yang, Y. R.,
1252 Klebert, M. K., Suessen, T., Teefey, S., Presti, R. M., Krammer, F., Kleinstein, S. H., Ward, A. B.
1253 & Ellebedy, A. H. Human germinal centres engage memory and naive B cells after influenza
1254 vaccination. *Nature* **586**, 127-132 (2020).
- 1255 72 Sachdeva, V., Husain, K., Sheng, J., Wang, S. & Murugan, A. Tuning environmental timescales
1256 to evolve and maintain generalists. *Proc. Natl. Acad. Sci. USA* **117**, 12693-12699 (2020).
- 1257 73 Wang, S. Optimal sequential immunization can focus antibody responses against diversity loss
1258 and distraction. *PLoS Comput. Biol.* **13**, e1005336 (2017).
- 1259 74 Molari, M., Eyer, K., Baudry, J., Cocco, S. & Monasson, R. Quantitative modeling of the effect of
1260 antigen dosage on B-cell affinity distributions in maturing germinal centers. *eLife* **9**, e55678
1261 (2020).
- 1262 75 Sprenger, K. G., Louveau, J. E., Murugan, P. M. & Chakraborty, A. K. Optimizing immunization
1263 protocols to elicit broadly neutralizing antibodies. *Proc. Natl. Acad. Sci. USA* **117**, 20077-20087
1264 (2020).
- 1265 76 Guthmiller, J. J. & Wilson, P. C. Harnessing immune history to combat influenza viruses. *Curr.*
1266 *Opin. Immunol.* **53**, 187-195 (2018).
- 1267 77 De Visser, J., Elena, S. F., Fragata, I. & Matuszewski, S. The utility of fitness landscapes and big
1268 data for predicting evolution. *Heredity* **121**, 401-405 (2018).
- 1269 78 Park, Y., Metzger, B. P. H. & Thornton, J. W. Epistatic drift causes gradual decay of predictability
1270 in protein evolution. *Science* **376**, 823-830 (2022).
- 1271 79 Gibson, D. G., Young, L., Chuang, R.-Y., Venter, J. C., Hutchison, C. A. & Smith, H. O. Enzymatic
1272 assembly of DNA molecules up to several hundred kilobases. *Nat. Methods* **6**, 343-345 (2009).
- 1273 80 Van Deventer, J. A., Kelly, R. L., Rajan, S., Wittrup, K. D. & Sidhu, S. S. A switchable yeast
1274 display/secretion system. *Protein Eng. Des. Sel.* **28**, 317-325 (2015).
- 1275 81 Engler, C., Kandzia, R. & Marillonnet, S. A one pot, one step, precision cloning method with high
1276 throughput capability. *PLoS One* **3**, e3647 (2008).
- 1277 82 Gietz, R. D. & Schiestl, R. H. High-efficiency yeast transformation using the LiAc/SS carrier
1278 DNA/PEG method. *Nat. Protoc.* **2**, 31-34 (2007).

- 1279 83 Chao, G., Lau, W. L., Hackel, B. J., Sazinsky, S. L., Lippow, S. M. & Wittrup, K. D. Isolating and
1280 engineering human antibodies using yeast surface display. *Nat. Protoc.* **1**, 755-768 (2006).
- 1281 84 Hoffmann, E., Neumann, G., Kawaoka, Y., Hobom, G. & Webster, R. G. A DNA transfection
1282 system for generation of influenza A virus from eight plasmids. *Proc. Natl. Acad. Sci. USA* **97**,
1283 6108-6113 (2000).
- 1284 85 Moody, M. A., Zhang, R., Walter, E. B., Woods, C. W., Ginsburg, G. S., McClain, M. T., Denny,
1285 T. N., Chen, X., Munshaw, S., Marshall, D. J., Whitesides, J. F., Drinker, M. S., Amos, J. D.,
1286 Gurley, T. C., Eudailey, J. A., Foulger, A., DeRosa, K. R., Parks, R., Meyerhoff, R. R., Yu, J.-S.,
1287 Kozink, D. M., Barefoot, B. E., Ramsburg, E. A., Khurana, S., Golding, H., Vandergrift, N. A.,
1288 Alam, S. M., Tomaras, G. D., Kepler, T. B., Kelsoe, G. *et al.* H3N2 Influenza infection elicits more
1289 cross-reactive and less clonally expanded anti-hemagglutinin antibodies than influenza
1290 vaccination. *PLoS One* **6**, e25797 (2011).
- 1291 86 Nguyen Ba, A. N., Cvijović, I., Rojas Echenique, J. I., Lawrence, K. R., Rego-Costa, A., Liu, X.,
1292 Levy, S. F. & Desai, M. M. High-resolution lineage tracking reveals travelling wave of adaptation
1293 in laboratory yeast. *Nature* **575**, 494-499 (2019).
- 1294 87 Moulana, A., Duplic, T., Phillips, A. M., Chang, J., Nieves, S., Roffler, A. A., Greaney, A. J., Starr,
1295 T. N., Bloom, J. D. & Desai, M. M. Compensatory epistasis maintains ACE2 affinity in SARS-CoV-
1296 2 Omicron BA. 1. *bioRxiv*, doi:10.1101/2022.06.17.496635 (2022).
- 1297 88 Regex (2013).
- 1298 89 Poelwijk, F. J., Socolich, M. & Ranganathan, R. Learning the pattern of epistasis linking genotype
1299 and phenotype in a protein. *Nat. Comm.* **10**, 4213 (2019).
- 1300 90 Pettersen, E. F., Goddard, T. D., Huang, C. C., Meng, E. C., Couch, G. S., Croll, T. I., Morris, J.
1301 H. & Ferrin, T. E. UCSF ChimeraX: Structure visualization for researchers, educators, and
1302 developers. *Protein Sci.* **30**, 70-82 (2021).
- 1303 91 Kimura, M. On the probability of fixation of mutant genes in a population. *Genetics* **47**, 713-719
1304 (1962).
- 1305 92 Kuraoka, M., Schmidt, A. G., Nojima, T., Feng, F., Watanabe, A., Kitamura, D., Harrison, S. C.,
1306 Kepler, T. B. & Kelsoe, G. Complex antigens drive permissive clonal selection in germinal centers.
1307 *Immunity* **44**, 542-552 (2016).
- 1308 93 Hagberg, A., Swart, P. & S Chult, D. (Sponsor Org.: USDOE).
- 1309 94 Adams, P. D., Grosse-Kunstleve, R. W., Hung, L.-W., Ioerger, T. R., McCoy, A. J., Moriarty, N.
1310 W., Read, R. J., Sacchettini, J. C., Sauter, N. K. & Terwilliger, T. C. PHENIX: building new
1311 software for automated crystallographic structure determination. *Acta Crystallogr. D* **58**, 1948-
1312 1954 (2002).
- 1313 95 McCoy, A. J., Grosse-Kunstleve, R. W., Adams, P. D., Winn, M. D., Storoni, L. C. & Read, R. J.
1314 Phaser crystallographic software. *J. Appl. Crystallogr.* **40**, 658-674 (2007).
- 1315 96 Emsley, P., Lohkamp, B., Scott, W. G. & Cowtan, K. Features and development of Coot. *Acta*
1316 *Crystallogr. D Biol. Crystallogr.* **66**, 486-501 (2010).

1317 97 Chen, V. B., Arendall, W. B., Headd, J. J., Keedy, D. A., Immormino, R. M., Kapral, G. J., Murray,
1318 L. W., Richardson, J. S. & Richardson, D. C. MolProbity: all-atom structure validation for
1319 macromolecular crystallography. *Acta Crystallogr. D* **66**, 12-21 (2010).
1320
1321

1322 **FIGURE SUPPLEMENTS**

1323



1324

1325

1326

1327

1328

1329

Figure 1 – figure supplement 1. CH65 mutation reversion. Isogenic measurements of $-\log K_D$ for CH65 with (18-mut) and without (16-mut) Q1E and S75A to MA90 (p -value = 0.82, t -stat = 0.26) and SI06 (p -value = 1.0, t -stat = 0.0); 'ns' designates a p -value > 0.05.

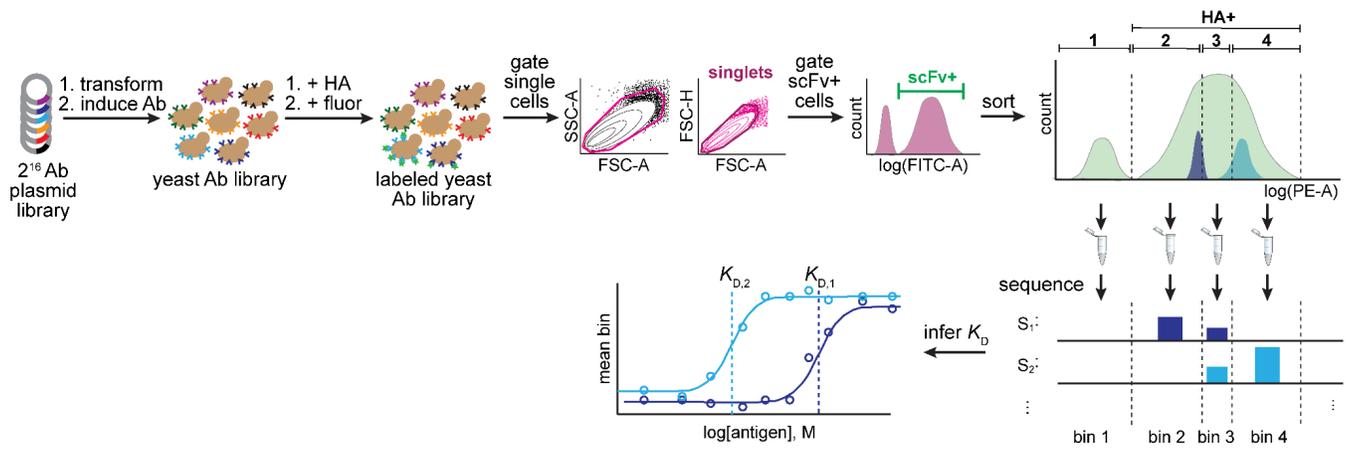
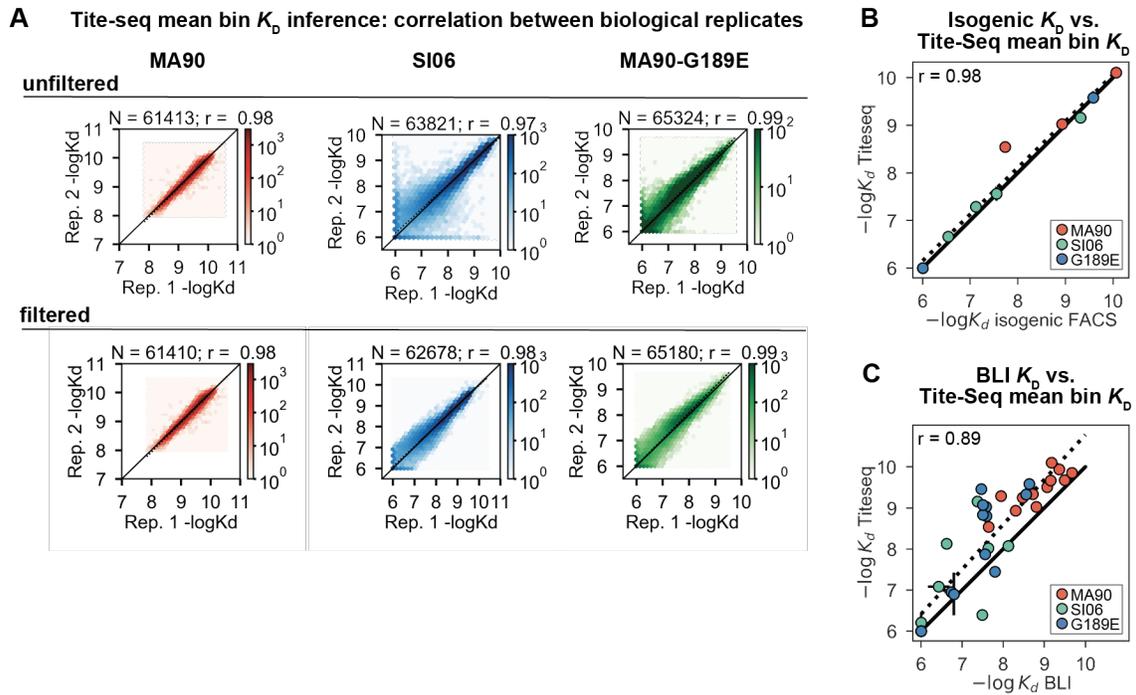


Figure 1 – figure supplement 2. Tite-seq workflow. Combinatorially complete ($N=2^{16}$ variants) antibody plasmid library is transformed into yeast and expression of antibodies is induced. Yeast antibody library is then labeled with HA (at varying concentrations) followed by fluorophores (FITC, which binds the Ab, and PE, which binds HA). Labeled yeast library is then gated to select single cells that express scFv. Scfv-positive cells are then sorted according to HA binding (PE fluorescence) into four bins. Bin 1 corresponds to all HA-negative cells, HA-positive cells are split evenly between the remaining three bins. Each bin is then sequenced to determine variant frequency in each bin. K_D is then inferred by fitting the mean bin each variant is observed in to the antigen concentration.

1330
1331
1332
1333
1334
1335
1336
1337
1338
1339
1340



1341 **Figure 1 – figure supplement 3. Tite-Seq K_D quality control and isogenic measurements. (A)** Correlation
 1342 between biological duplicate Tite-Seq K_D measurements before (top) and after (bottom) removing genotypes with -
 1343 $\log K_D$ differing by more than one-log between replicates. The latter set of measurements were used for all
 1344 downstream analyses. N indicates the number of variants plotted, r indicates the correlation between replicates. **(B)**
 1345 Correlation between Tite-Seq $-\log K_D$ measurements and isogenic fluorescence-based $-\log K_D$ measurements for a
 1346 subset of mutants to one of the three antigens, as indicated in key. Error bars indicate the SEM between replicates
 1347 and are generally smaller than the points. **(C)** Correlation between Tite-Seq $-\log K_D$ measurements and BLI $-\log K_D$
 1348 measurements for a subset of mutants to one of the three antigens, as indicated in key. Error bars indicate the SEM
 1349 between replicates (for Tite-Seq) and the SE of the fit (for BLI) and are generally smaller than the points.

1350
 1351
 1352

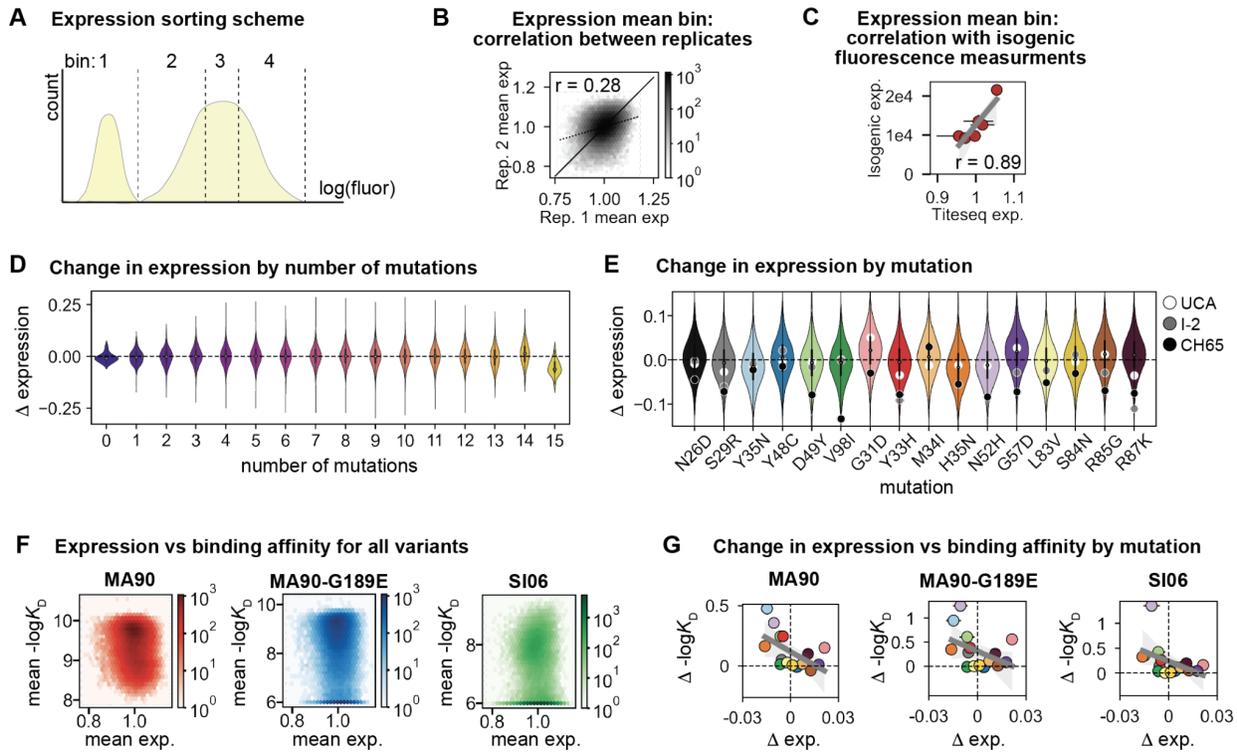
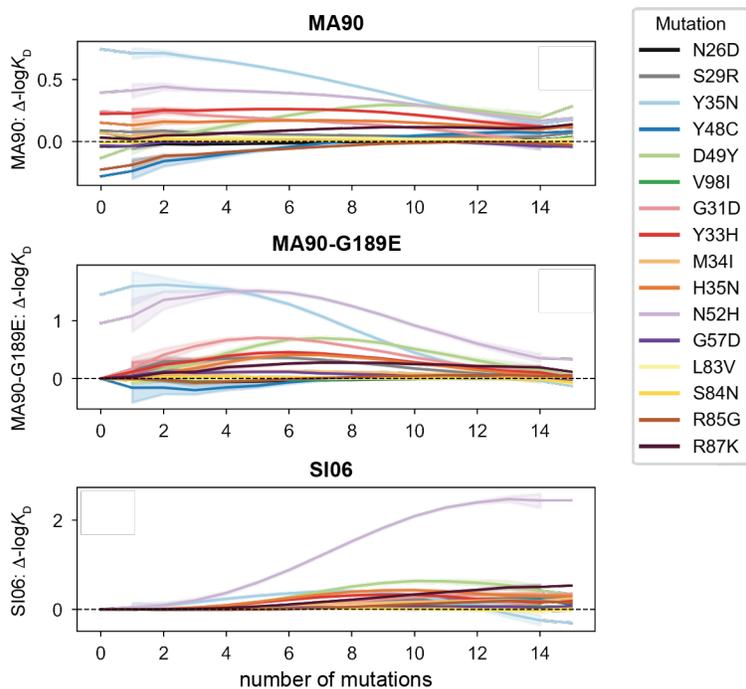


Figure 1 – figure supplement 4. CH65 library expression. (A) Sorting scheme for scFv expression. Library was sorted into four bins, each comprising 25% of the total population, along the log(fluorescence) axis corresponding to expression (FITC). (B) Correlation between Tite-Seq biological replicate measurements of expression for all variants in the CH65 library. (C) Correlation between mean Tite-Seq expression measurement and mean isogenic expression measurement for select variants. (D) Change in expression resulting from mutation, as a function of the number of other mutations present. (E) Change in expression resulting from each mutation. Each violin contains 32,768 points corresponding to the effect of that mutation on the 32,768 other genetic backgrounds. White, gray, and black points show the impact of the mutation on expression on the UCA, I-2, and CH65 genetic backgrounds, respectively. (F) Relationship between expression and binding affinity for all variants in the CH65 library. (G) Relationship between mean change in expression and mean change in binding affinity resulting from each of the 16 mutations in CH65. Mutations are colored as in (E).

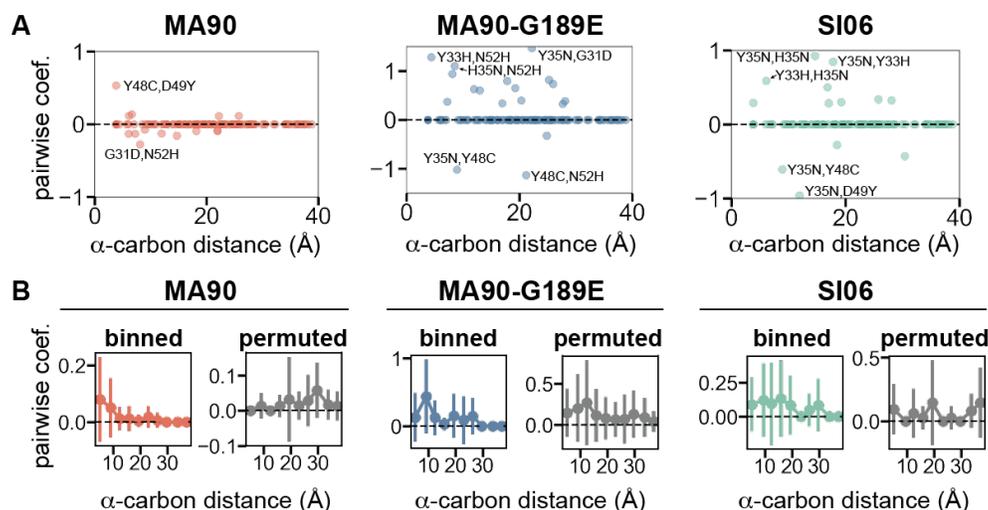
1353
1354
1355
1356
1357
1358
1359
1360
1361
1362
1363
1364
1365
1366
1367



1368
1369
1370
1371
1372
1373
1374
1375

Figure 2 – figure supplement 1. Change in $-\log K_b$ resulting from each mutation as a function of the number of other mutations present. Line represents mean, shading represents 95% confidence interval over all genetic backgrounds.

1376



1377

1378

1379

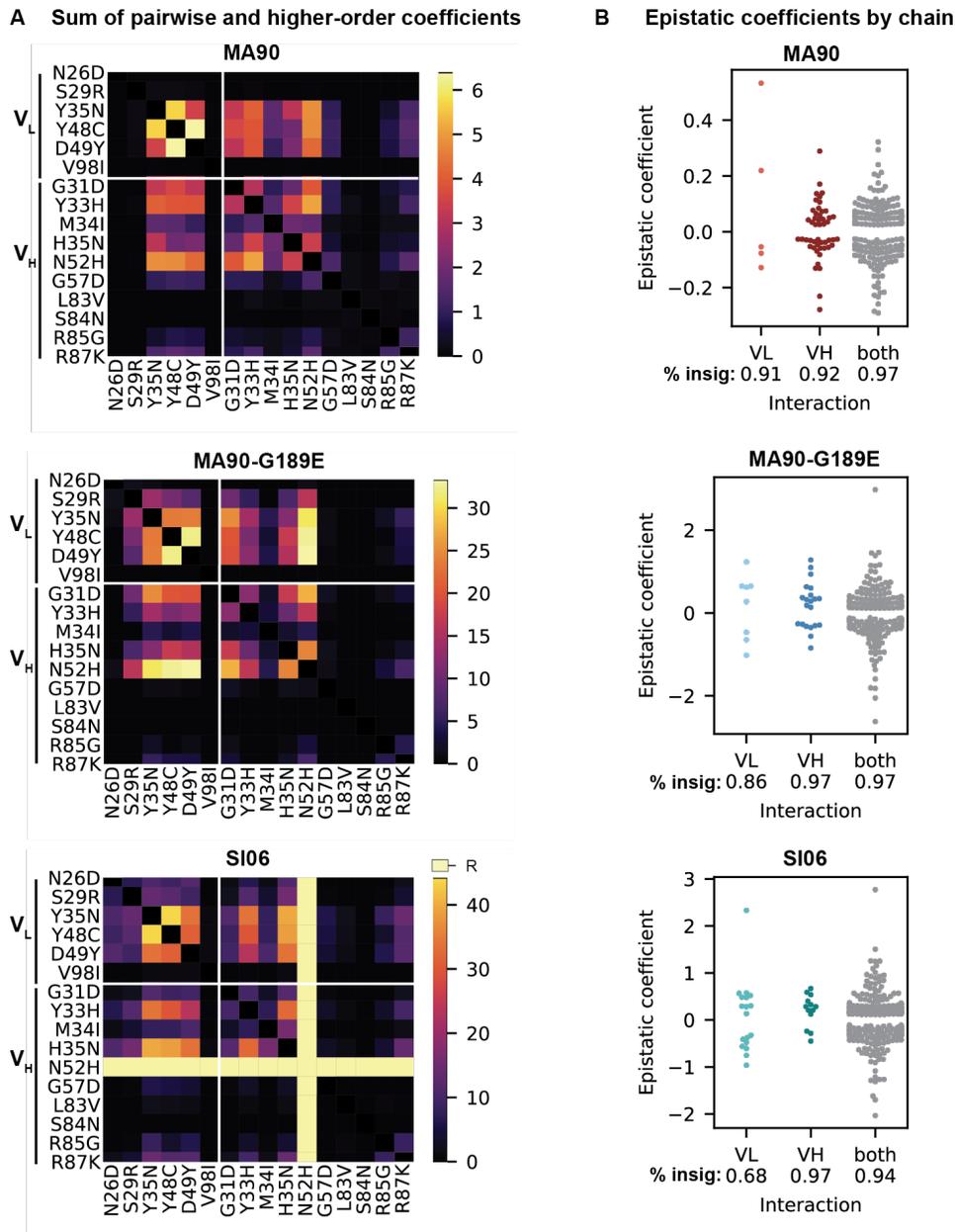
1380

1381

1382

1383

1384



1385

1386

1387

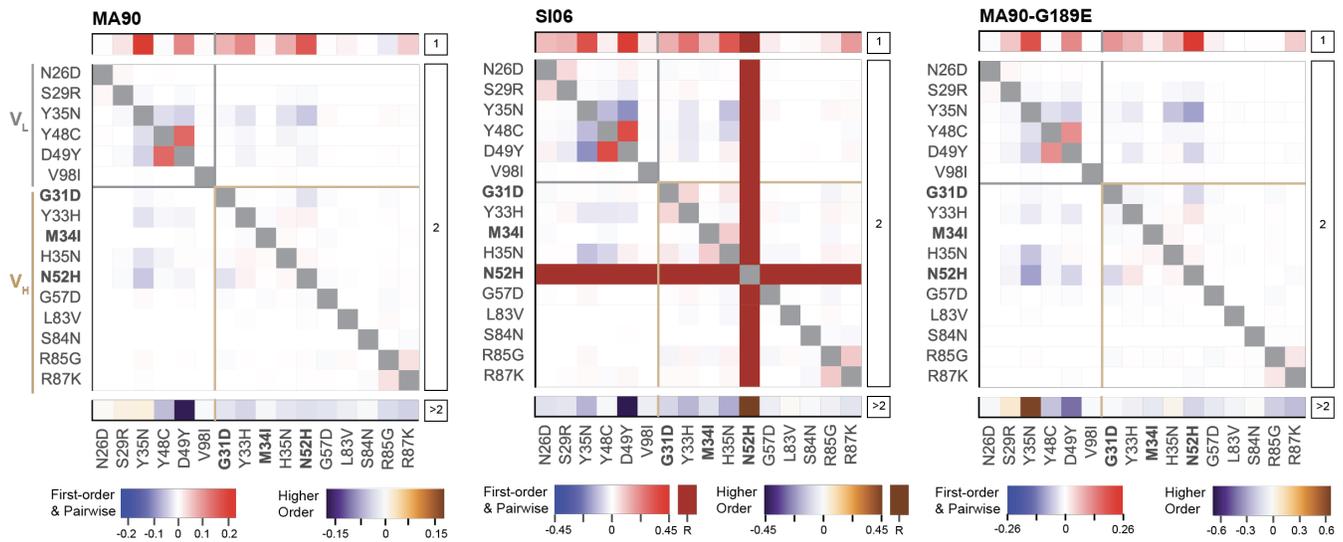
1388

1389

1390

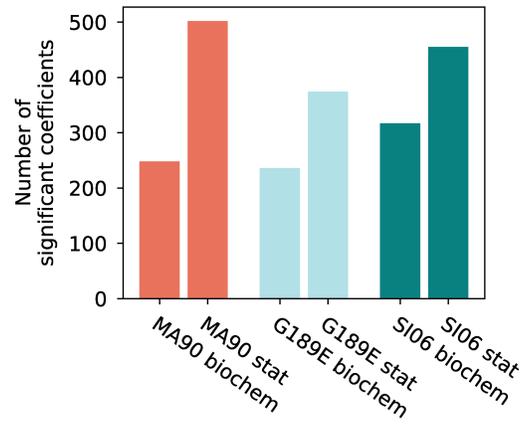
1391

Figure 3 – figure supplement 2. Biochemical epistasis within heavy and light chains and between chains. (A) Sum of absolute value of statistically significant (Bonferroni-corrected p -value < 0.05) pairwise and higher-order coefficients for MA90, MA90-G189E, and SI06. **(B)** Significant epistatic coefficients between mutations in the light chain (VL), heavy chain (VH) or between mutations spread across both chains (both). Percentage of insignificant coefficients is indicated below each swarm plot.



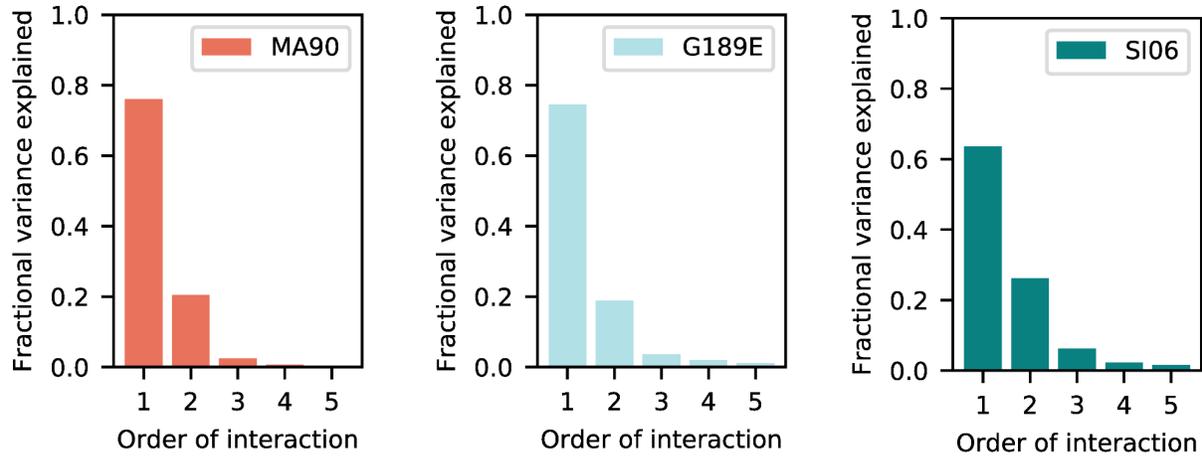
1392
1393
1394
1395
1396
1397
1398
1399

Figure 3 – figure supplement 3. Epistatic coefficients for statistical model of epistasis. First-order, pairwise, and higher-order mutational effects for each of the 16 mutations inferred from the optimal order model for each antigen. Higher-order effects are reported as a sum. Mutations present in I-2 are shown in bold. 'R' indicates that the mutation is required for binding (defined as being present in $\geq 90\%$ of binding variants) and is thus excluded from the epistasis inference.



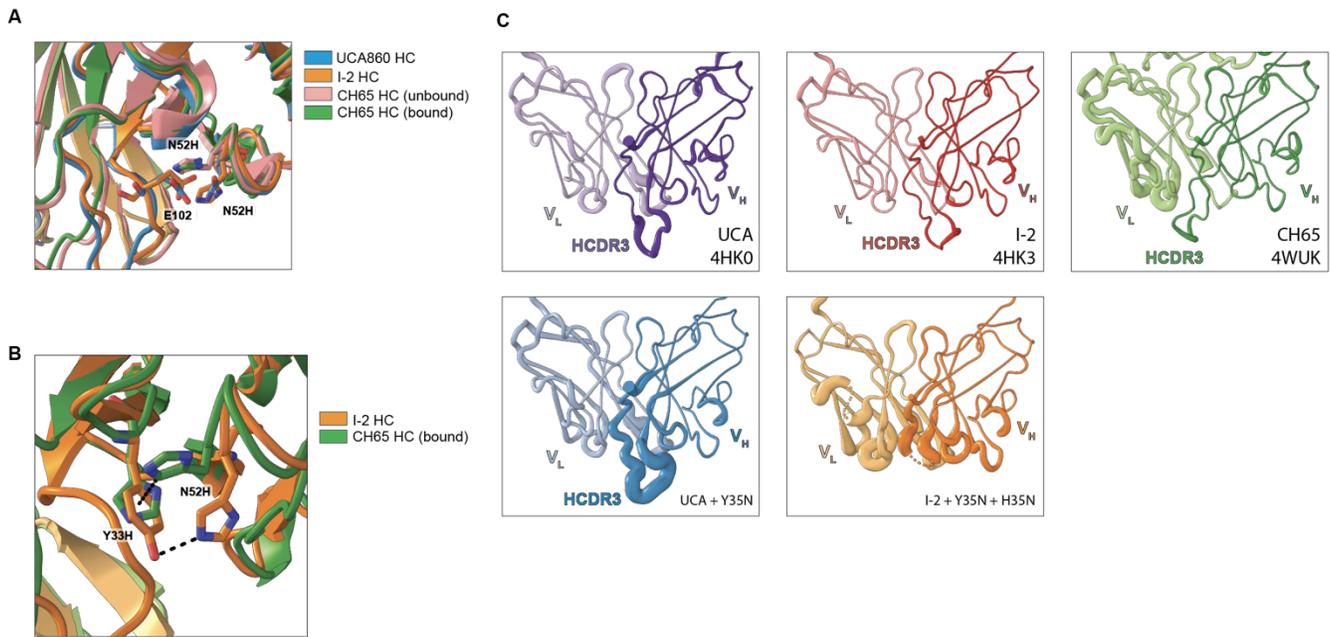
1400
1401
1402
1403
1404
1405

Figure 3 – figure supplement 4. Comparison of coefficients in biochemical and statistical models. Total number of statistically significant coefficients is plotted for each antigen and epistatic model (Bonferroni-corrected p -value < 0.05).



1406
1407
1408
1409

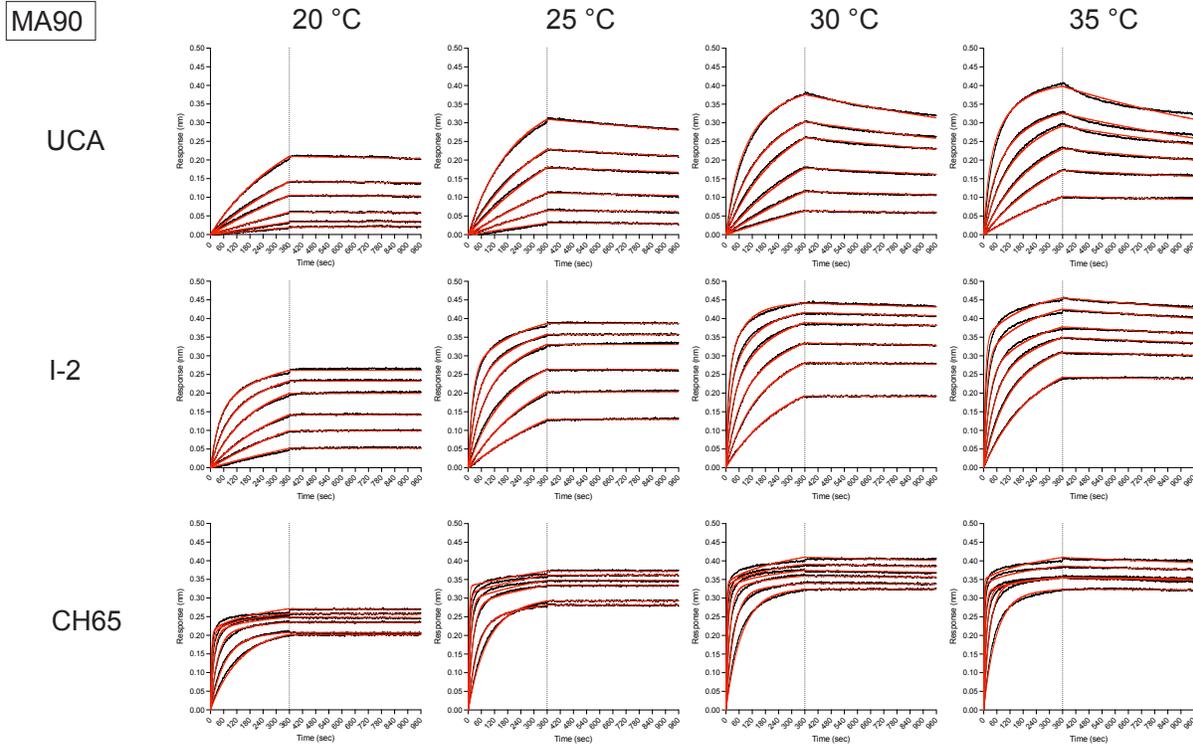
Figure 3 – figure supplement 5. Variance partitioning of statistical epistasis coefficients by order of interaction.



1410
1411
1412
1413
1414
1415
1416
1417
1418
1419
1420
1421

Figure 4 – figure supplement 1. (A) The mutation N52H in CH65 (PDB 4WUK (unbound) and 5UGY (bound)) clashes with E102 in the HCDR3 conformations observed in the unbound crystal structures of the UCA (PDB 4HK0) and I-2 (PDB 4HK3). **(B)** Residue 52H moves to π -stack with residue 33 in a T configuration in CH65 compared to hydrogen bonding between 52H and 33Y in unbound I-2. **(C)** Unbound Fab structures of several variants in the CH65 lineage. Cartoon volume is scaled by B factors. Previously reported structures show that the HCDR3 conformation in the UCA and I-2 is different than that in CH65, which matches the bound conformation (top). Although the UCA with the Y35N mutation confers affinity to MA90-G189E, the HCDR3 is not in the binding conformation and has exceedingly high B factors (bottom left). Similarly, although the I-2 with the mutations Y35N and H35N confer affinity to SI06, the HCDR3 lacked sufficient density and also had high B factors (bottom middle).

1422



1423

1424

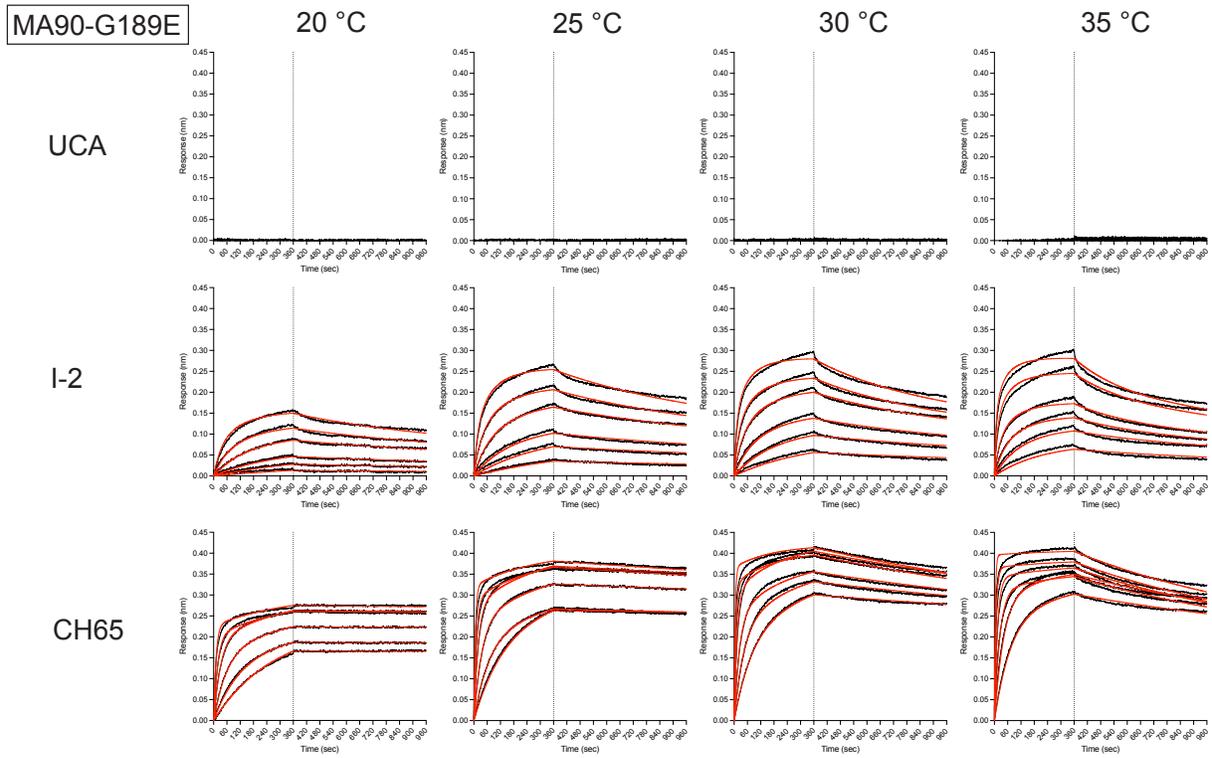
1425

1426

1427

1428

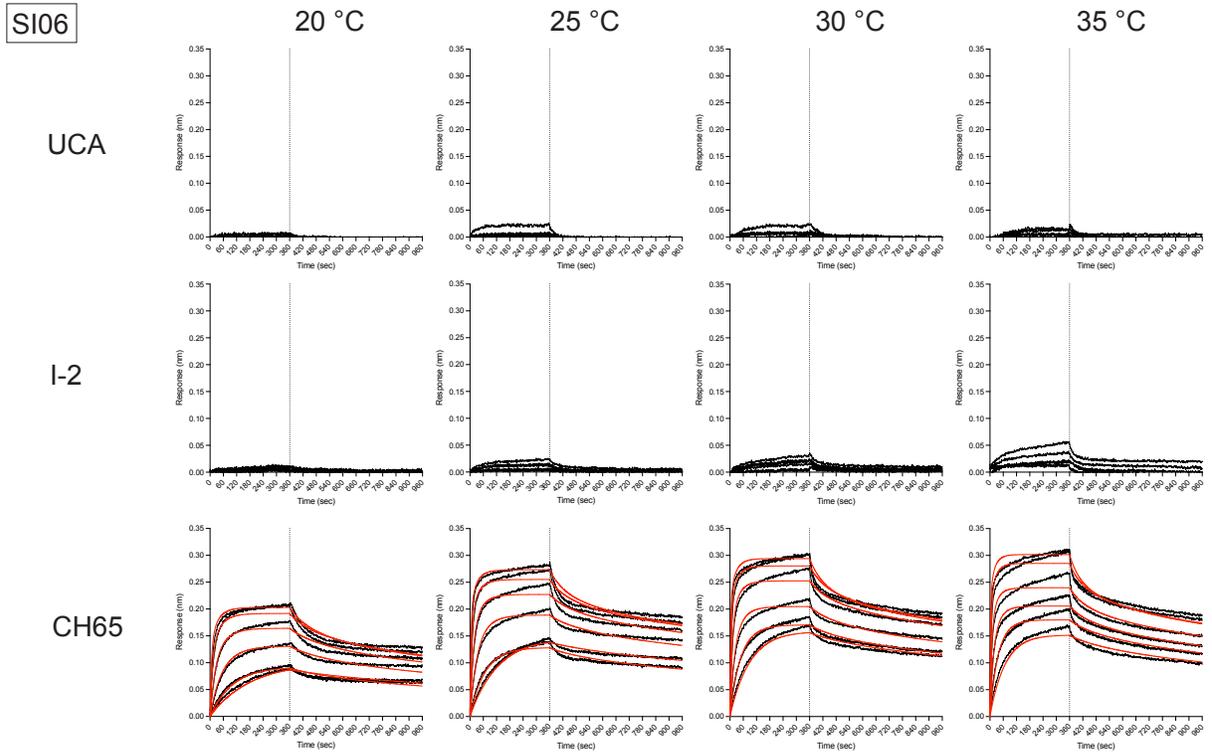
Figure 4 – figure supplement 2. Representative biolayer interferometry binding traces against MA90 for the indicated antibodies (left) and temperatures (top). Black is the processed data and red is the global curve fit using the bivalent analyte model.



1429
1430
1431
1432
1433
1434

Figure 4 – figure supplement 3. Representative biolayer interferometry binding traces against MA90-G189E for the indicated antibodies (left) and temperatures (top). Black is the processed data and red is the global curve fit using the bivalent analyte model. For the UCA, there was no detectable binding.

1435



1436

1437

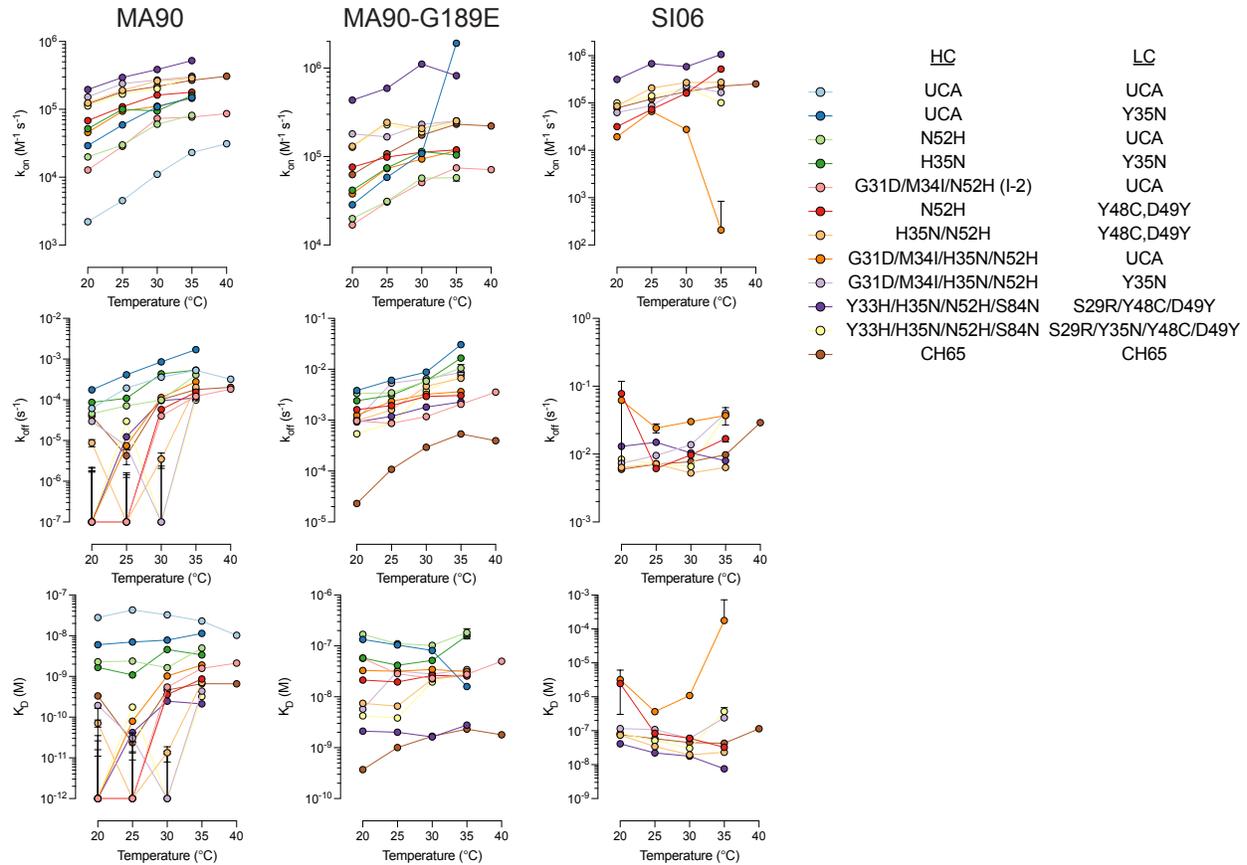
1438

1439

1440

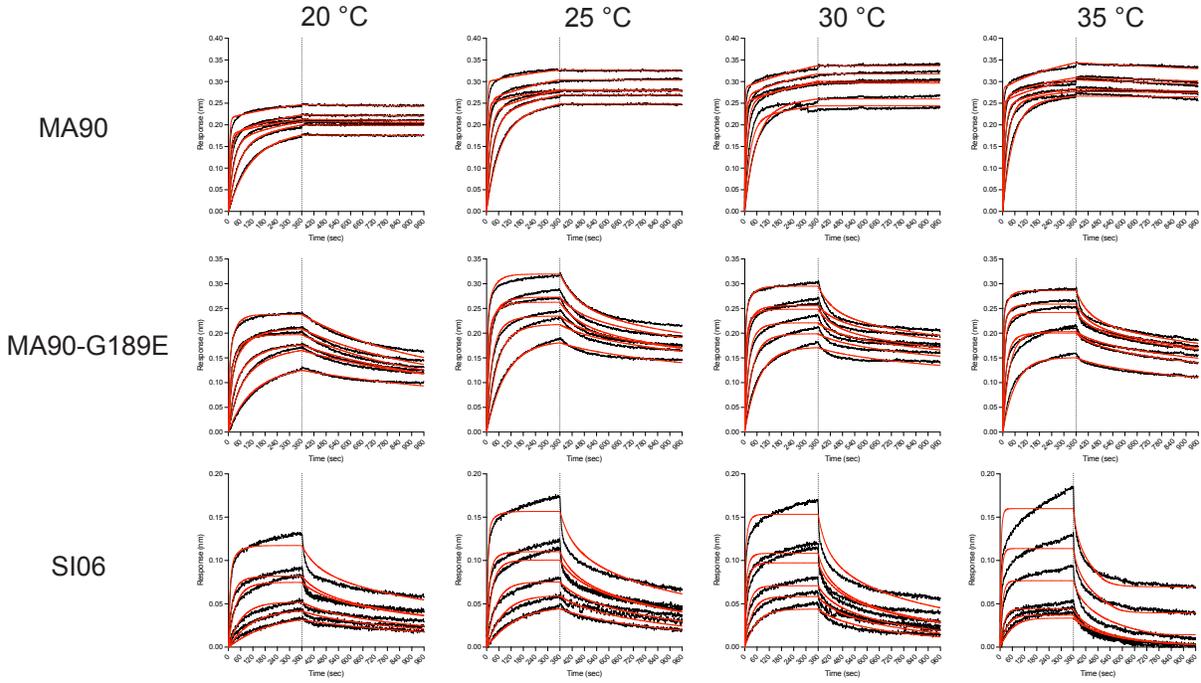
1441

Figure 4 – figure supplement 4. Representative biolayer interferometry binding traces against SI06 for the indicated antibodies (left) and temperatures (top). Black is the processed data and red is the global curve fit using the bivalent analyte model. For the UCA and I-2, any signal was too weak for analysis.



1442 **Figure 4 – figure supplement 5.** Summary of association rates (top), dissociation rates (middle), and dissociation
 1443 constants (bottom) measurements made by biolayer interferometry for the indicated antigens (top). Error bars
 1444 represent the standard error for kinetic parameters derived from global curve fitting with a bivalent analyte model
 1445 using the analysis software supplied with the instrument (Sartorius Data Analysis HT 12.0.2.59). For some high
 1446 affinity variants, the dissociation time was too short to accurately measure the dissociation rate against MA90
 1447 accurately, especially at lower temperatures (left) resulting in inaccurate dissociation rates with large errors.
 1448 Antibodies that did not bind MA90-G189E (middle) or SI06 (right) were not included in the plots.

HC: G31D/M34I/H35N/N52H LC: Y35N



1449
1450
1451
1452
1453
1454

Figure 4 – figure supplement 6. Biolayer interferometry binding traces for the antibody variant containing the I-2 mutations (G31D, M34I, and N52H) in addition to H35N and Y35N for the indicated antigens (left) and temperatures (top). Weak but detectable binding is observed for SI06.

	UCA Y35N Fab (unbound)	I-2 Y35N H35N Fab (unbound)
Data Collection		
Resolution (Å)	50 - (2.07 - 1.95)	50 - (2.86 - 2.70)
Wavelength (Å)	0.97918	0.97918
Space Group	C121	C121
Unit cell dimensions (a, b, c) (Å)	124.547, 70.707, 86.934	127.724, 70.652, 75.759
Unit cell angles (α , β , γ) (°)	90, 126.957, 90	90, 119.354, 90
I/σ	17.23 (2.13)	7.39 (2.08)
R_{meas} (%)	5.2 (72.9)	23.3 (113.1)
CC _{1/2} (%)	99.9 (80.0)	97.8 (78.4)
Completeness (%)	98.3 (97.0)	96.4 (90.8)
Number of observed reflections	167769 (26758)	87005 (13683)
Number of unique reflections	43266 (6872)	15770 (2360)
Redundancy	3.88 (3.89)	5.5 (5.8)
Refinement		
Resolution (Å)	49.76 - 1.954 (2.024 - 1.954)	39.41 - 2.7 (2.797 - 2.7)
Reflections used in refinement	43263 (4194)	15760 (1400)
Reflections used for R_{free}	2000 (194)	1580 (136)
R_{work} (%)	18.53 (28.49)	24.45 (37.27)
R_{free} (%)	21.59 (33.5)	28.32 (48.39)
Ramachandran favored/allowed (%)	96.55 / 2.99	95.87 / 3.4
Ramachandran outliers (%)	0.46	0.73
Rmsd bond lengths (Å)	0.017	0.003
Rmsd bond angles (°)	1.74	0.59
Average B-factor	49.43	62.33
PDB ID	8EK6	8EKH

1455
1456
1457

Figure 4 – figure supplement 7. X-ray data collection and refinement statistics for unbound Fabs.

1458

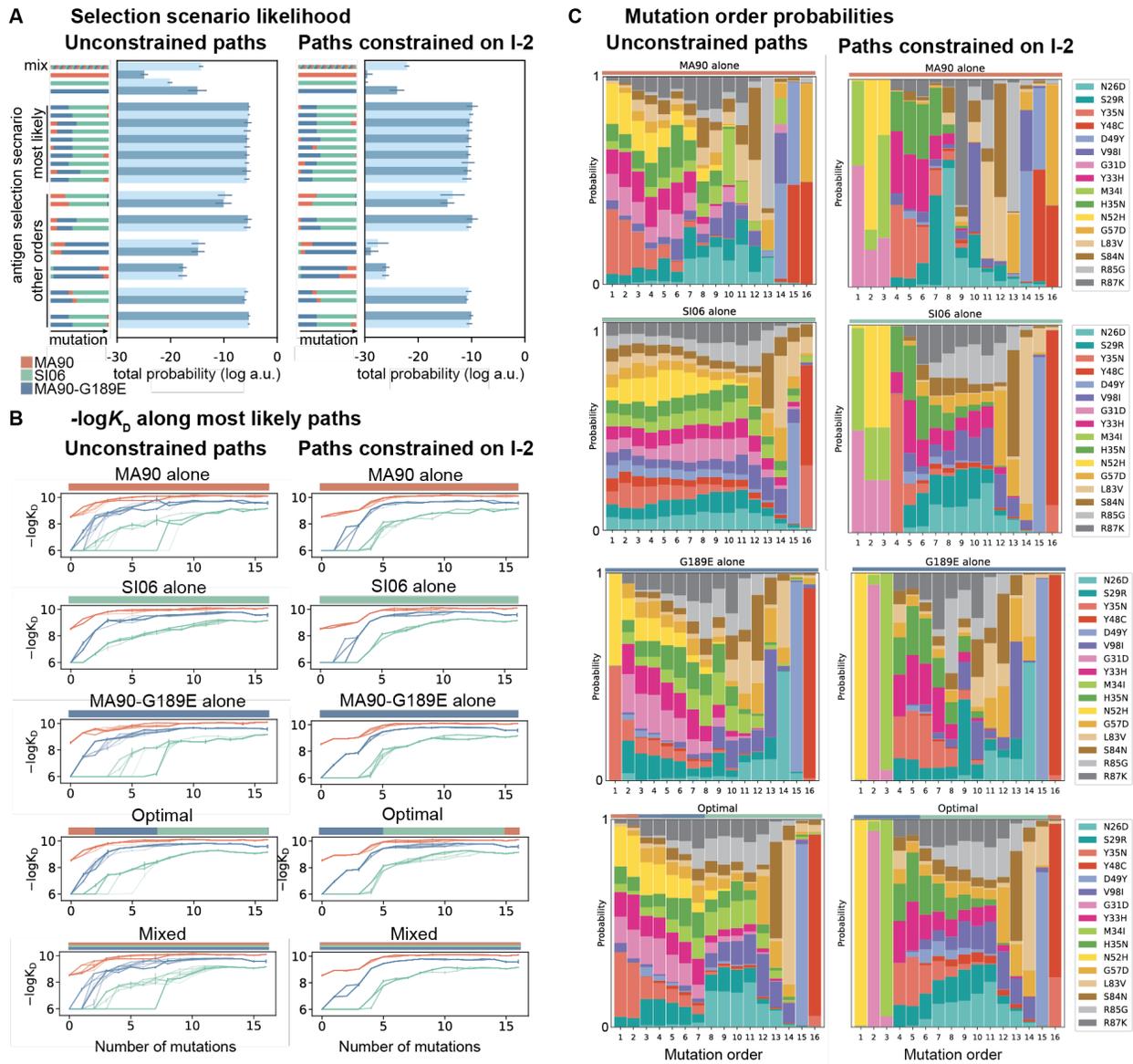
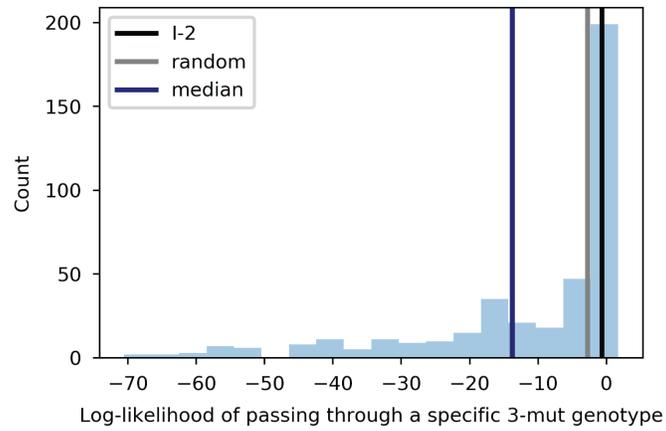


Figure 5 – figure supplement 1. Antigen selection scenarios and likely mutational pathways with MA90, SI06, and MA90-G189E. (A) Selection scenario likelihood. Total probability of all mutational paths (left) or all paths that pass through I-2 (right) assuming specific antigen selection scenarios are shown. **(B)** $-\log K_D$ for 25 most likely paths under designated antigen selection scenarios are shown with (right) and without (left) the constraint of passing through I-2. **(C)** Probability of each mutation occurring at a specific order under select antigen selection scenarios, with (right) and without (left) the constraint of passing through I-2.

1459
1460
1461
1462
1463
1464
1465
1466
1467
1468



1469
1470
1471
1472
1473
1474
1475

Figure 5 – figure supplement 2. Likelihood of passing through specific 3-mutation intermediates. Histogram indicates number of 3-mutation variants with a given log-likelihood, under the unconstrained moderate selection model presented in Figure 5. The log-likelihood corresponding to I-2, the expectation for a 3-mutation genotype chosen at random (1/560), and the median across all 3-mutation genotypes are indicated as vertical lines on the plot.